

# LEPTONS IN THE PROTON & IMPLICATIONS TO LHC PHENOMENOLOGY

Luca Buonocore

University of Zurich, INFN-sezione di Napoli

*L. Buonocore, P. Nason, F. Tramontano and G. Zanderighi* [[JHEP 08 \(2020\) 08, 019](#)]

*L. Buonocore, U. Haisch, P. Nason, F. Tramontano and G. Zanderighi* [[2005.06475](#)]



University of  
Zurich<sup>UZH</sup>

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Istituto Nazionale di Fisica Nucleare  
SEZIONE DI NAPOLI  
Gruppo Collegato di Salerno

# INTRODUCTION

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- Hadrons are usually viewed as “broad band beams” of **coloured** particles (quarks and gluons). Hard processes described by factorisation formulae in terms of convolutions with partonic PDFs

$$\sigma(h_1 + h_2 \rightarrow V + X) = \sum_{ab} \int dx_1 dx_2 f_{a/h_1}(x_1, \mu_F) f_{b/h_2}(x_2, \mu_F) \hat{\sigma}_{ab \rightarrow V+X}(\hat{s}, \mu_R) + \dots$$

- Indeed hadrons are made of **constituent/valence quarks** and (soft and collinear) QCD radiation is copiously produced (**sea of gluons and quarks**)
- Order of quark and gluon PDFs

$$(\alpha_s L)^k \quad \alpha_s (\alpha_s L)^k \quad L \equiv \ln \frac{Q^2}{\Lambda^2}$$

- $\Lambda$  is a characteristic **hadronic scale**.
- Since  $L \sim 1/\alpha_s$ , all the contributions becomes relevant!

# INTRODUCTION: MOTIVATIONS

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- QCD radiation is certainly the dominant effect. When **electromagnetism** is taken into account, **photons and eventually leptons can be radiated** starting from quarks.
- Being down by **two powers** of electromagnetic  $\alpha$  (naive estimate), leptonic luminosities are indeed very small compared to the ones of the other partons inside the proton.
- It might be interesting to look at lepton initiated processes in hadronic colliders
  - in principle, all lepton-lepton combinations are available (and in a broad energy spectrum): potential to measure **exotic SM processes**
  - potential to look at exotic **BSM physics**
- LHC will take data for the next 15-20 years: **explore all of its possibilities!**

# INTRODUCTION: MOTIVATIONS

- A crucial aspect which prevented so far to fully explore the phenomenology offered by lepton initiated processes is **the lack of a precise determination of the lepton densities**

arXiv:hep-ph/9406235v1 3 Jun 1994

## SINGLE LEPTOQUARK PRODUCTION AT HADRON COLLIDERS

J. Ohnemus<sup>1</sup>, S. Rudaz<sup>2</sup>,  
T.F. Walsh<sup>2</sup> and P.M. Zerwas<sup>3</sup>

<sup>1</sup> Physics Department, University of California, Davis CA 95616, USA

<sup>2</sup> School of Physics and Astronomy, University of Minnesota, Minneapolis MN 55455, USA

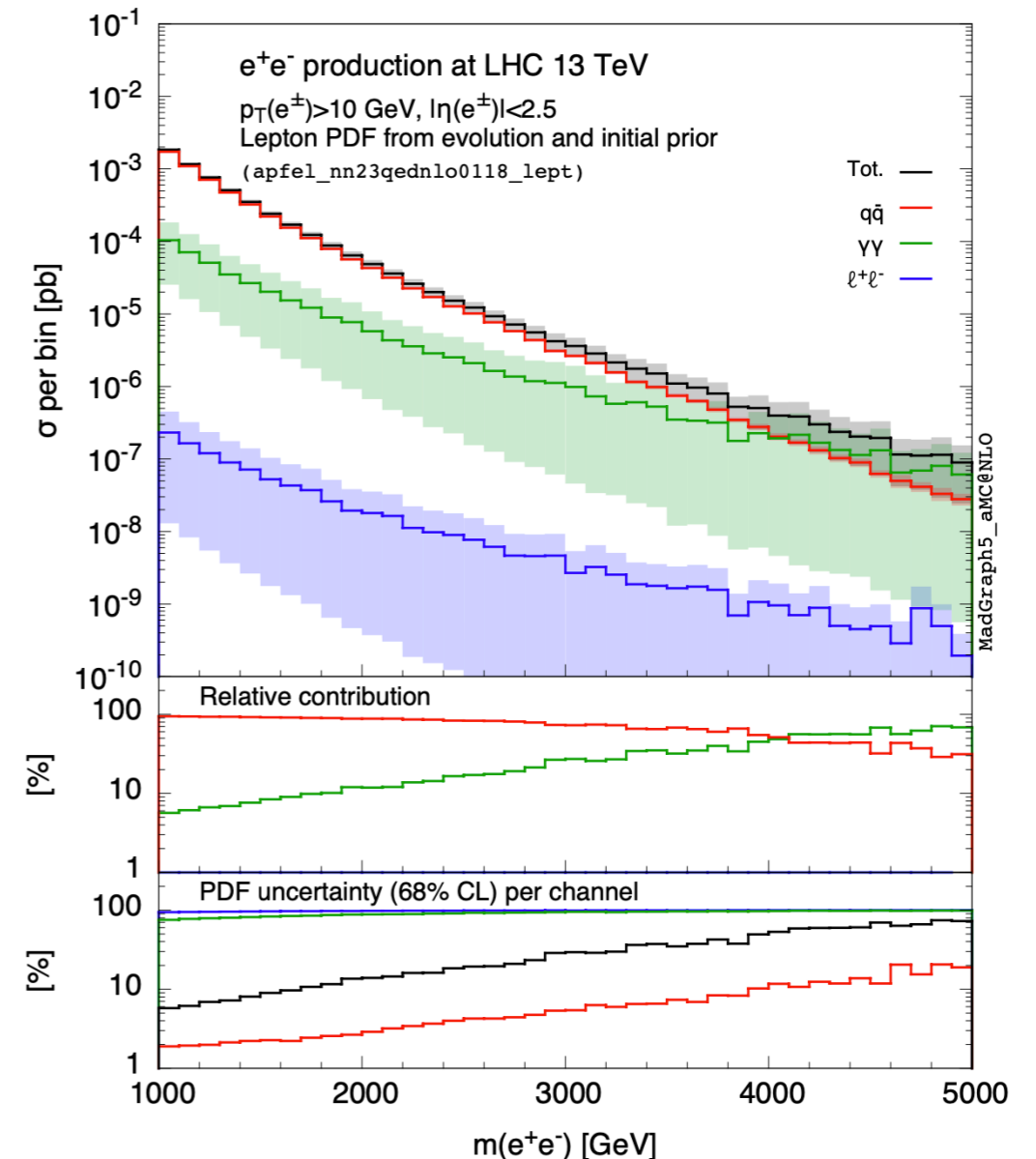
<sup>3</sup> Deutsches Elektronensynchrotron DESY, D-22603 Hamburg, FRG

### Abstract

Leptoquarks can be produced in pairs by gluon-gluon fusion and quark-antiquark annihilation at hadron colliders. While HERA is the proper machine for single production of ( $eu$ ) and ( $ed$ ) type leptoquarks, the flavor species of ( $\mu u$ ), ( $\mu d$ ) and ( $\tau u$ ), ( $\tau d$ ) type leptoquarks can be produced at hadron colliders very efficiently. Besides exploiting gluon-quark collisions, leptoquarks can also be produced singly by colliding the quarks in one proton beam with leptons  $e, \mu, \tau$  generated by splitting photons which are radiated off the quarks in the other proton beam. For Yukawa couplings of the size  $\alpha$  leptoquark masses up to about 300 GeV can be generated at the Tevatron while the LHC can produce leptoquarks with masses up to about 3 TeV. [Leptoquarks involving heavy quarks can be produced singly at a lower rate, determined by the heavy flavor flux in the proton beam.]

1994 paper: very interesting, but almost forgotten...

[Bertone, Carrazza, Pagani, Zaro, *JHEP* 11 (2015) 194]



# OUTLINE

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- Lepton PDF formula and the LUXlep set
- LHC Phenomenology
- New limits on minimal scalar LeptoQuarks models
- Conclusions

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# LEPTON PDF FORMULA and THE LUXlep SET

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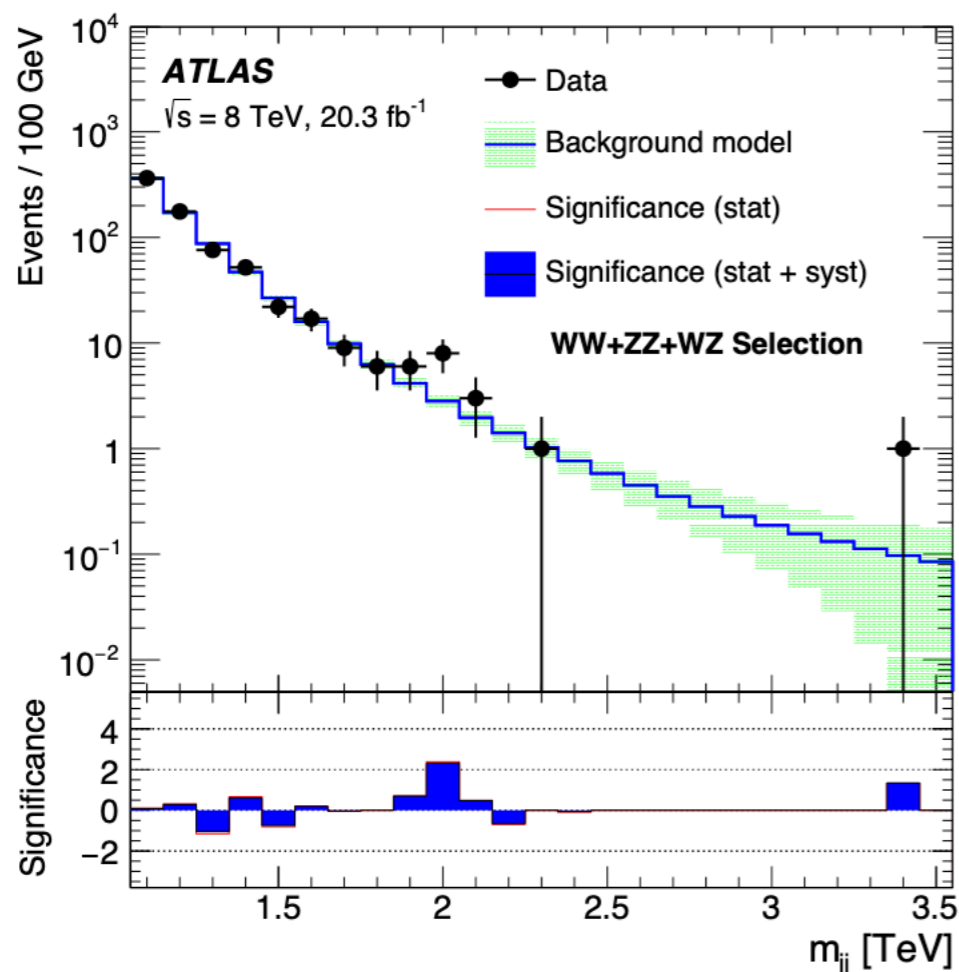
# The “LUX” APPROACH for the PHOTON PDF

- **LUX breakthrough** in 2016-2017

[Manohar, Nason, Salam, Zanderighi, *Phys.Rev.Lett.* 117 (2016) 24, 242002]

[Manohar, Nason, Salam, Zanderighi, *JHEP* 12 (2017) 046 ]

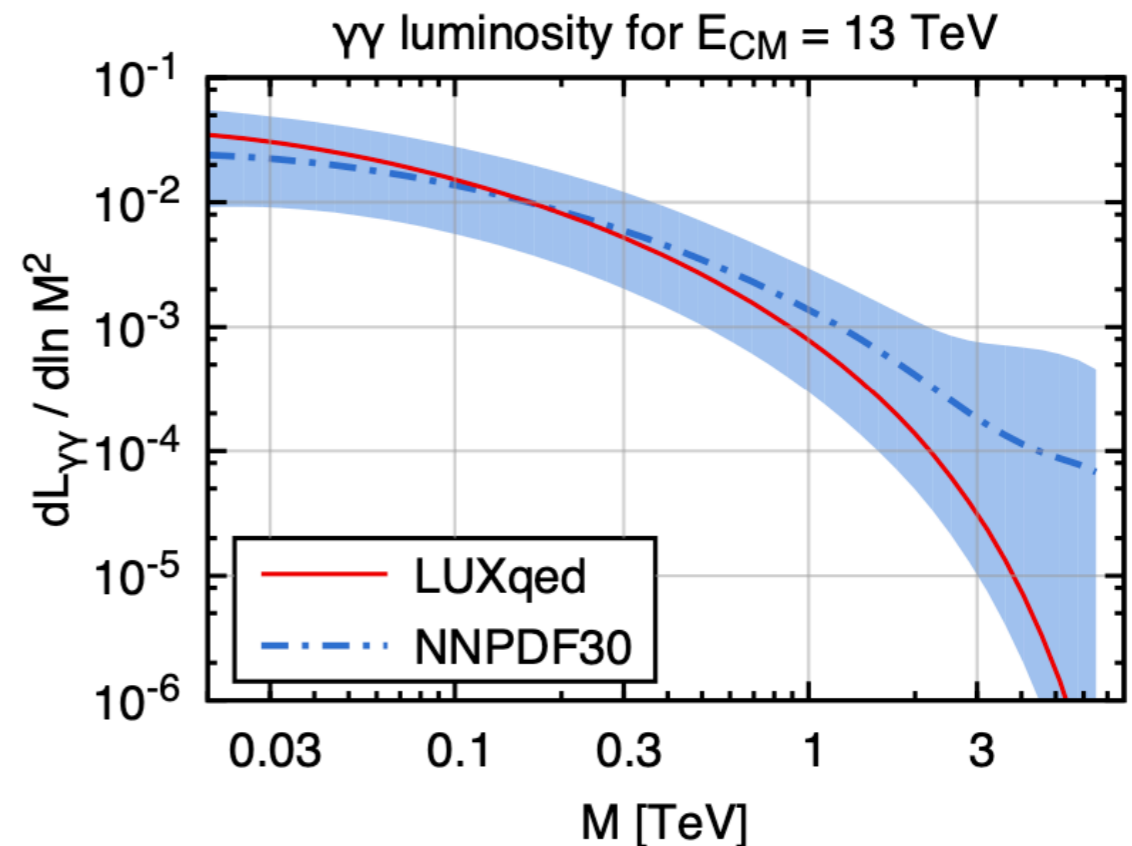
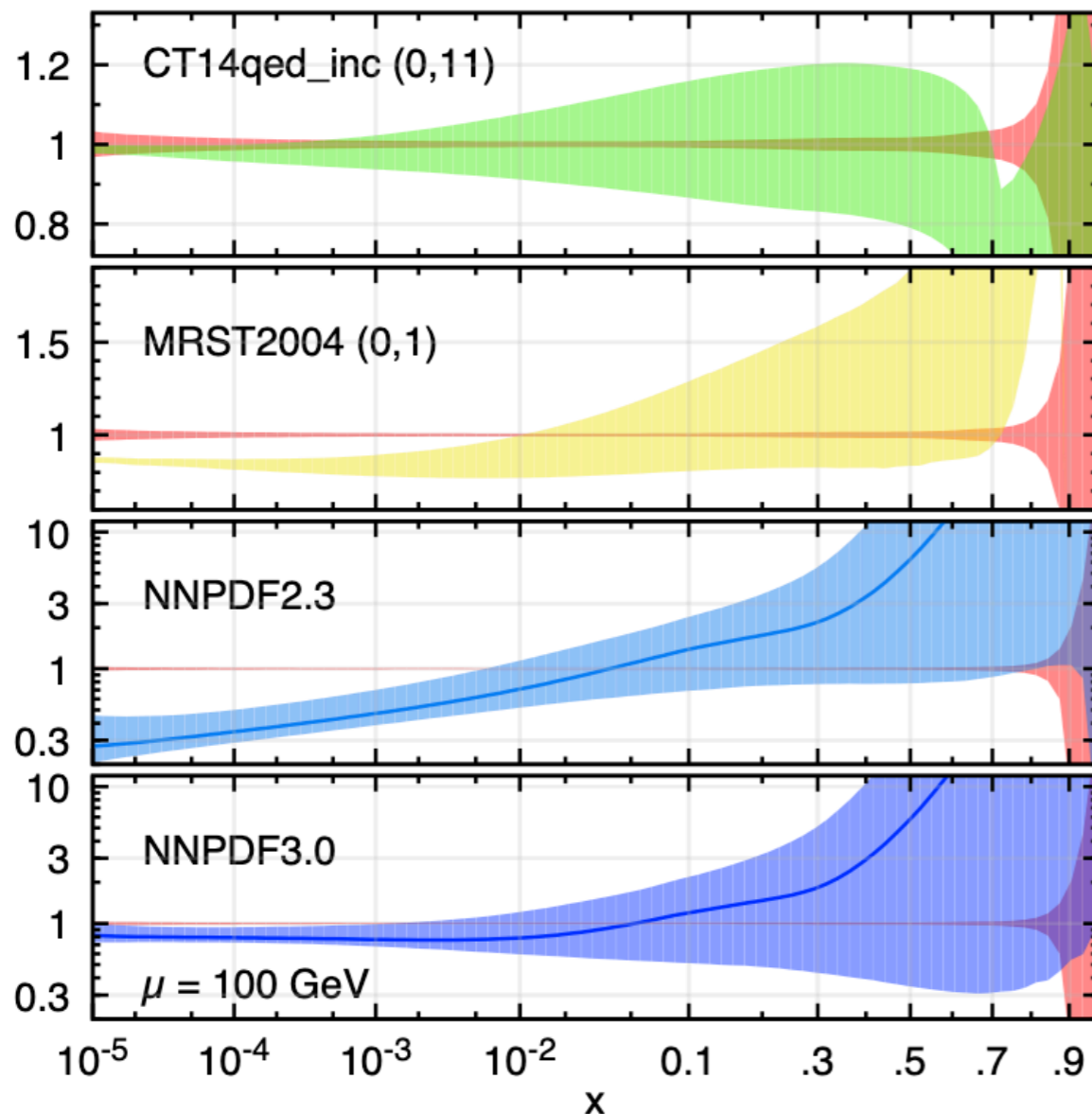
- determination of the photon density within  $\sim 5\%$  **uncertainty**
- **different motivations:** uncertainty on the photon induced processes started to dominate the production of **high mass objects**



## ATLAT boosted jets analysis (2015):

- 2 TeV excess in boson pair production
- **Not confirmed in 13 TeV run**
- The worry was that at very high scales gluon and quarks soften due to AP evolution.
- **Photons mostly stay the same:**  
importance of elastic contribution at low- $Q^2$

# Before the “LUX” and after ...



- Order of magnitude improvements in the knowledge of the photon content of proton ( paradigmatic case: comparison with the “agnostic” photon of NNPDF30)
- LUX approach can be used also for leptons (at order  $\alpha^2$ )!



# THE LUX APPROACH in a NUTSHELL

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- Relate the photon PDF to the electro-production structure functions and form factors for electron-proton scattering
  - physical ground: photon equivalent approximation and **virtual quanta** method, **collinear factorisation**
  - the computation **can be systematically improved** including higher order corrections to reach the desired accuracy goal
- Make use of the good quality data **(already) available**
  - electro-production structure functions measured in a **wide range of energies**
  - allow to **constrain** the photon PDF from **low- to high- $Q^2$**
- In general, no need to perform a global fit analysis
  - a new set which includes the photon can be produced starting from an existing one (which does not include it).

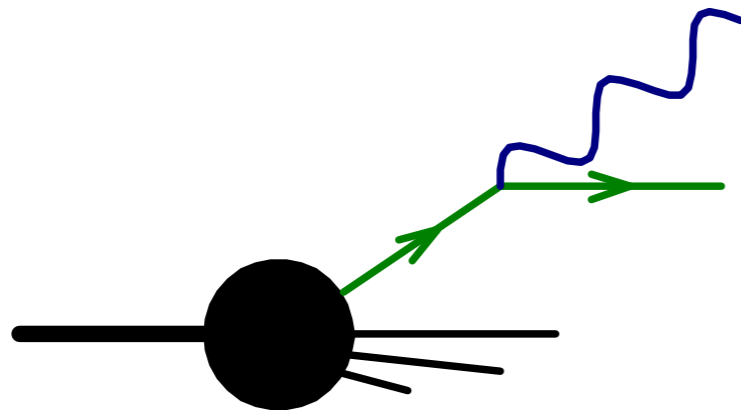
# (PHYSICAL) COUNTING SCHEME for photons

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- Let's start from quark and gluon again ...

$$(\alpha_s L)^k \quad \alpha_s (\alpha_s L)^k \quad L \equiv \ln \frac{Q^2}{\Lambda^2}$$

- The photon PDF is **down by a factor  $\alpha L$**  relatively to the quark density ( the powers of  $(\alpha_s L)^k \sim 1$  are always understood in the following)
- $\alpha L$  is not of order one! This complicates the relative importance of the couplings



$\alpha L$  (collinear-enhanced term)

**LO contribution**

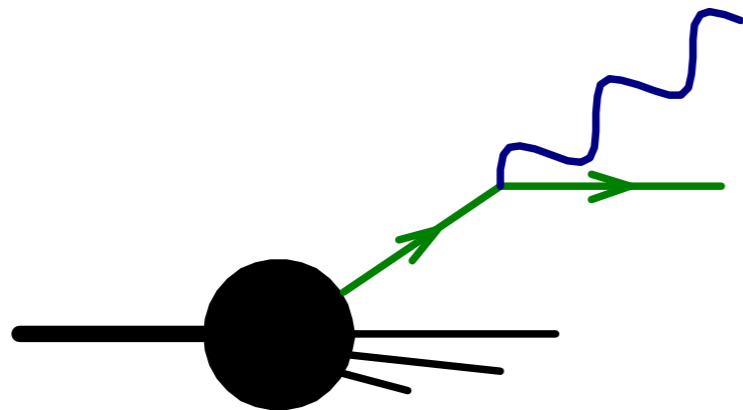
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$\alpha$  (non-collinear-enhanced term)

down by  $1/L \sim \alpha_s$  wrt LO

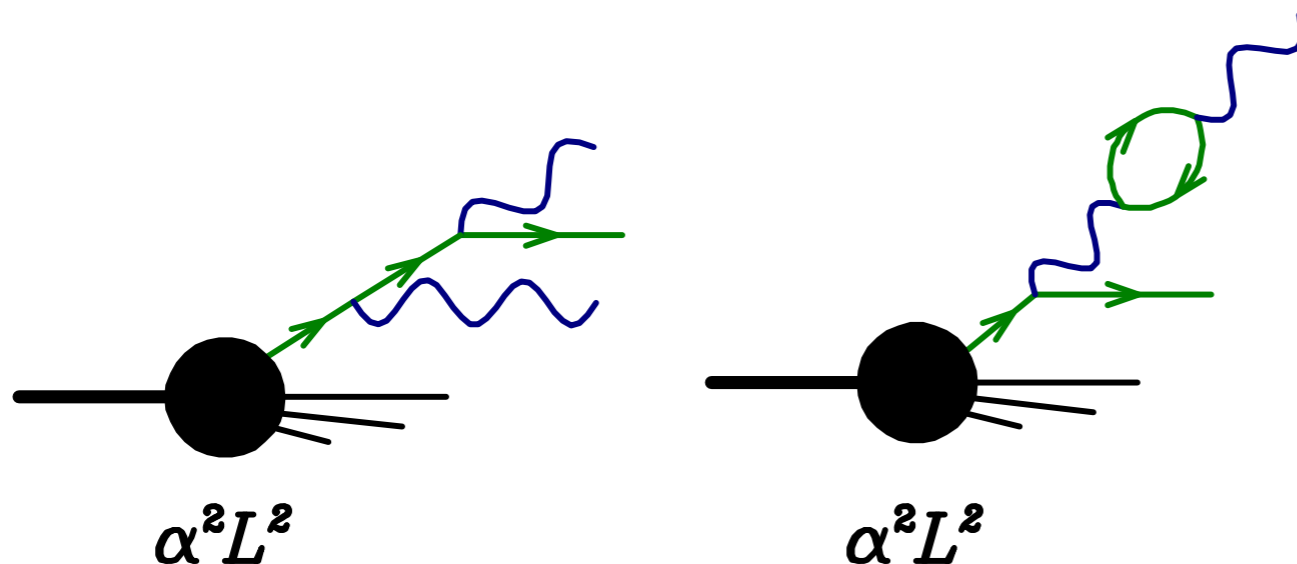
**NLO contribution**

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Assuming  $\alpha \sim \alpha_s^2$

down by  $\alpha L \sim \alpha_s$  wrt LO

**NLO contributions**

# (PHYSICAL) COUNTING SCHEME for leptons

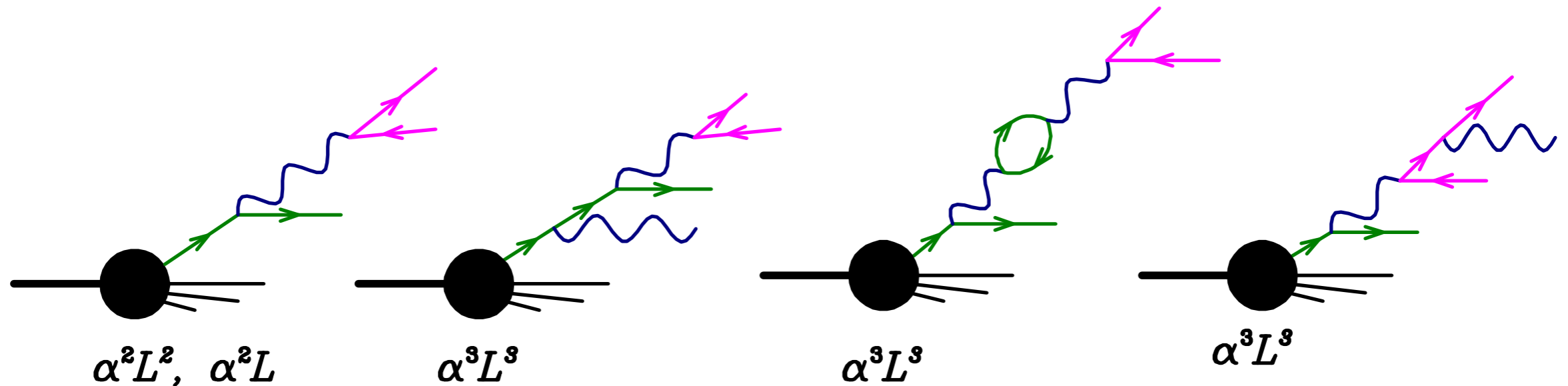
- Photon PDF

$$f_\gamma : \quad \begin{array}{c} \text{LO} \quad \text{NLO} \\ \alpha L \quad \alpha \quad \alpha^2 L^2 \quad \dots \end{array}$$

- Terms down by  $\alpha$  with respect to LO are neglected (NNLO in our counting)

- Similarly for lepton PDFs

$$f_\ell : \quad \begin{array}{c} \text{LO} \quad \text{NLO} \\ \alpha^2 L^2 \quad \alpha^2 L \quad \alpha^3 L^3 \quad \dots \end{array}$$



# APPLICATION TO THE LEPTON PDF CASE

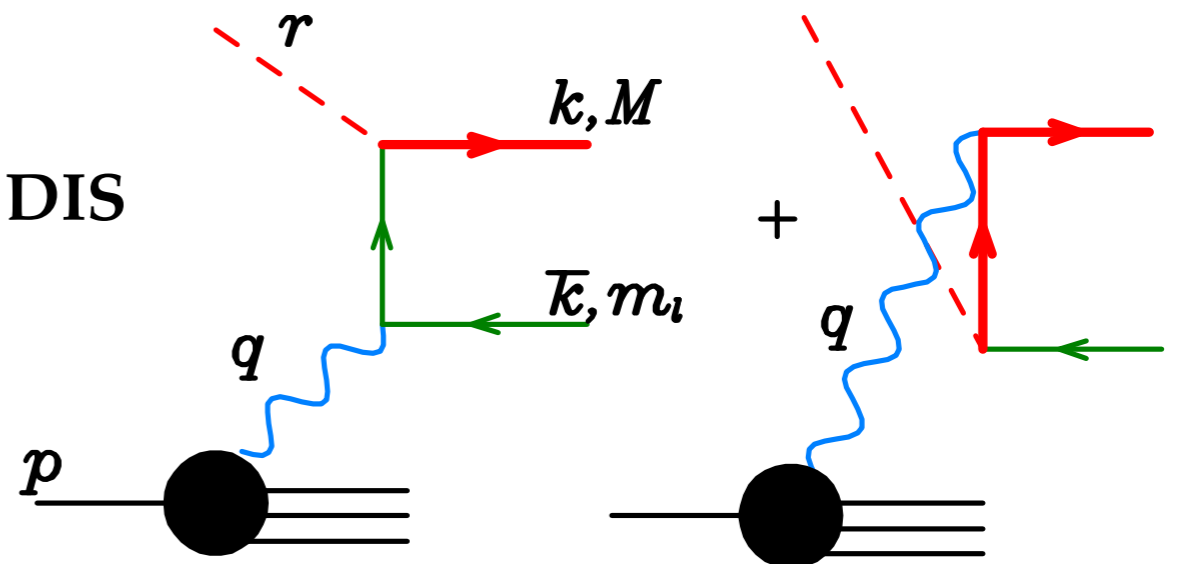
- Consider a fictitious BSM scalar probe that couples only to leptons and allow a flavour changing transitions to a BSM heavy lepton  $L$  of mass  $M$

$$\mathcal{L} \sim \phi_0 \bar{L} l + \text{h.c.}$$

- The cross section can be computed as in DIS

$$\sigma = \frac{1}{4p \cdot r} \int \frac{d^4 q}{(2\pi)^4} \frac{1}{Q^4} L^{\mu\nu}(r, q) (4\pi) W_{\mu\nu}(p, q)$$

Leptonic Tensor



$$W_{\mu\nu}(p, q) = F_1 \left( -g_{\mu\nu} + \frac{q_\mu q_\nu}{q^2} \right) + \frac{F_2}{p \cdot q} \left( p_\mu - \frac{p \cdot q}{q^2} q_\mu \right) \left( p_\nu - \frac{p \cdot q}{q^2} q_\nu \right)$$

Hadronic Tensor (scattering of virtual photon)

$$Q^2 = -q^2 > 0, x_{\text{bj}} = \frac{Q^2}{2p \cdot q}$$

$F_1(x_{\text{bj}}, Q^2), F_2(x_{\text{bj}}, Q^2)$  are the proton structure functions

# DIS-like COMPUTATION

- Integration domain

$$\int \frac{dE_{cm}^2}{2\pi} \frac{1}{4p \cdot r} \frac{1}{16\pi^2 E_{cm}^2} \int_x^{1 - \frac{2xm_P}{E_{cm}}} dz \int_{\frac{m_P^2 x^2}{1-z}}^{\frac{E_{cm}^2(1-z)}{z}} \left( \frac{dQ^2}{Q^2} \right) \alpha^2 \quad E_{cm}^2 = (r - q)^2$$

logarithmic integral

dominated at low  $Q^2$

- Sketch of the structure of the integral function

$$F_i \times P(Q^2, m_P^2, m_\ell^2, \dots) \log \frac{M^2}{Q^2} + F_i \times R(Q^2, m_P^2, m_\ell^2, \dots)$$

explicit logarithm of  $Q^2$

- P and R do not include logarithmic enhanced terms in  $Q^2$

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	<i>P</i>	<i>R</i>
$\frac{m_P^2}{Q^2}, \frac{m_\ell^2}{Q^2}$	<i>L</i>	no log
$\mathcal{O}(1)$	<i>L</i> <sup>2</sup>	<i>L</i>
$\mathcal{O}(Q^2)$	<del>no log</del>	<del>no log</del>

formally of order  $\alpha^2$  (NNLO)

no log  $\equiv$  no log-enhanced



# DIS-like COMPUTATION

- Integration domain

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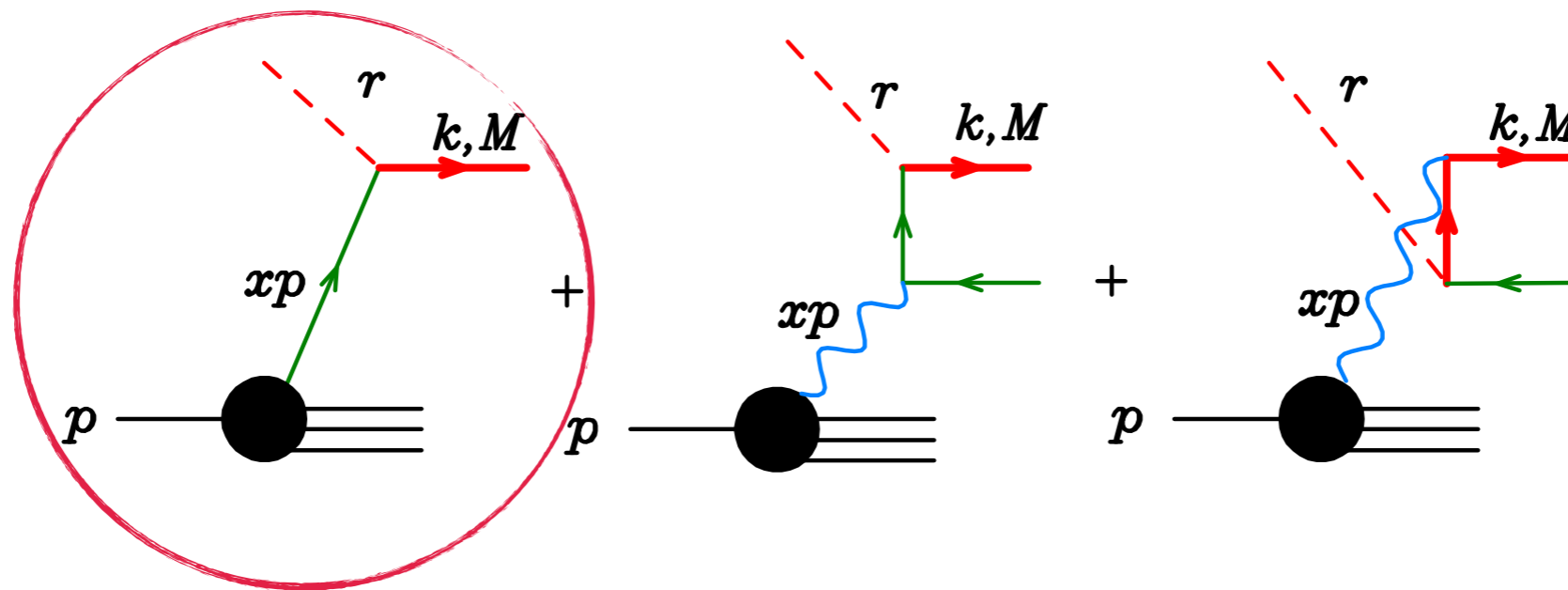
$$F_i \times P(Q^2, m_P^2, m_\ell^2, \dots) \log \frac{M^2}{Q^2} + F_i \times R(Q^2, m_P^2, m_\ell^2, \dots)$$

Terms proportional to  $\frac{m_P^2}{Q^2}, \frac{m_\ell^2}{Q^2}$  are the **only exception** to our counting rule: *Keep them!*

- they are formally NNLO, but are **dominated by small  $Q^2$  values**
- being insensitive to the high scale  $M \approx \mu_F$ , **scale variation does not capture the uncertainty** associated to those contributions
- they are **universal**. No new terms of this kind can be generated at higher orders

# PARTON MODEL CALCULATION

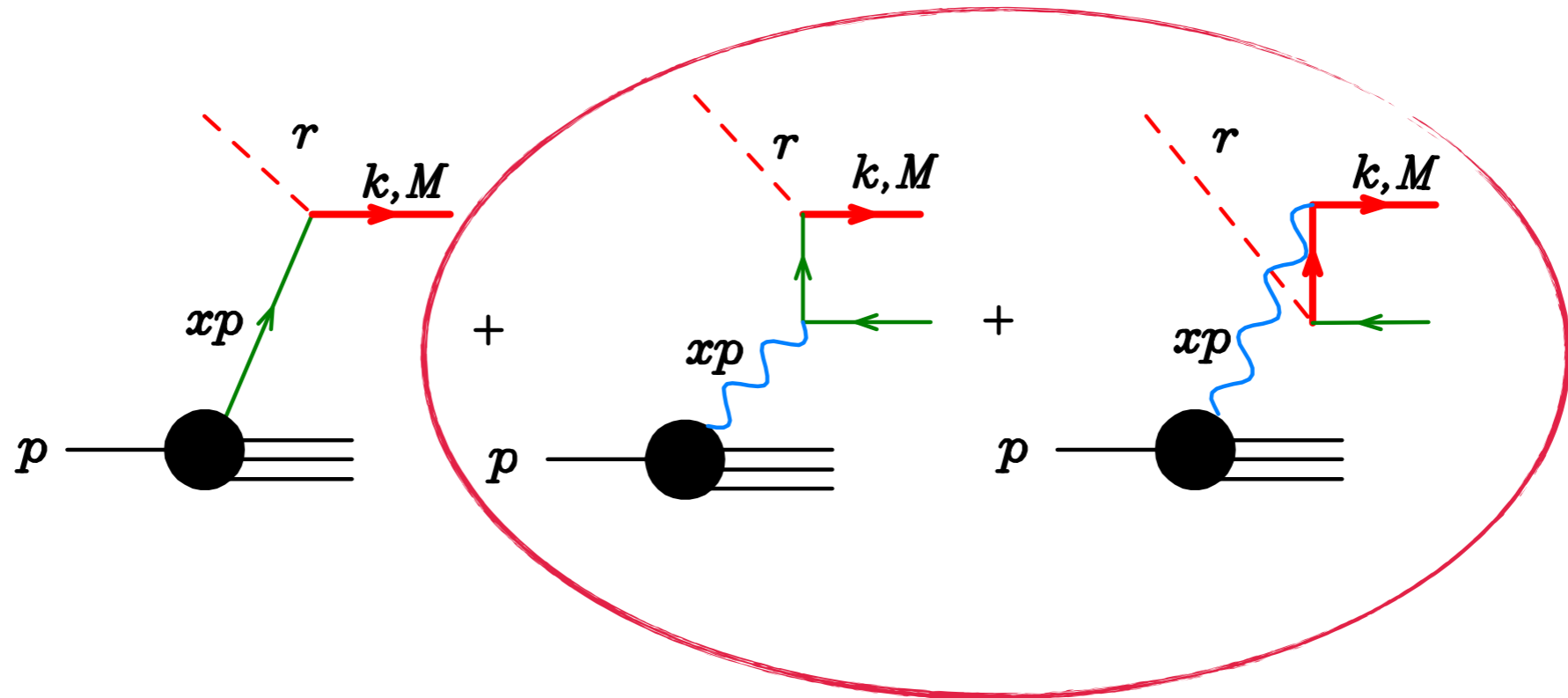
2. The cross section can be computed applying the collinear factorisation



$$\frac{\sigma}{\sigma_B} = \int dx f_\ell(x, \mu_F^2) \delta(Sx - M^2)$$

# PARTON MODEL CALCULATION

2. The cross section can be computed applying the collinear factorisation



$$\frac{\sigma}{\sigma_B} = \int dx f_\ell(x, \mu_F^2) \delta(Sx - M^2) \quad z_\ell = \frac{M^2}{xS}$$

$$+ \frac{\alpha}{2\pi} \frac{1}{M^2} \int_{\frac{M^2}{S}}^1 dx f_\gamma(x, \mu_F^2) \left\{ z_\ell P_{l\gamma}(z_\ell) \left[ \log \frac{M^2}{\mu_F^2} + \log \frac{(1 - z_\ell)^2}{z_\ell^2} \right] + 4z_\ell^2(1 - z_\ell) \right\}$$

# LEPTON PDF FORMULA

- Compare the two cross sections for the probe process & **Retain** only terms that contribute within our accuracy
- $\alpha^3 L^3$  contributions **not included** here

$$x_\ell f_\ell(x_\ell, \mu_F^2) = \left(\frac{1}{2\pi}\right)^2 \int_{x_\ell}^1 \frac{dx}{x} z_\ell \int_x^1 \frac{dz}{z} \int_{\frac{m_p^2 x^2}{1-z}}^{\frac{\mu_F^2}{1-z}} \frac{dQ^2}{Q^2} \alpha^2(Q^2)$$

matching  
neglecting  $\mathcal{O}(E_{\text{cm}}^2/\mu_F^2)$

$L^2$ -enhanced  
terms

$$\left\{ P_{\ell\gamma}(z_\ell) \log \frac{\mu_F^2}{(1-z_\ell)z_\ell \left(Q^2 + \frac{m_\ell^2}{z_\ell(1-z_\ell)}\right)} \left[ F_2 \left( z P_{\gamma q}(z) + \frac{2m_p^2 x^2}{Q^2} \right) - F_L z^2 \right] \right.$$

$$+ F_2 \left[ 4(z-2)^2 z_\ell(1-z_\ell) - (1+4z_\ell(1-z_\ell)) z P_{\gamma q}(z) \right] \quad \left. \begin{array}{l} L\text{-enhanced} \\ \text{terms} \end{array} \right\}$$

sub-leading  
terms

$$\left. \begin{array}{l} + F_L z^2 P_{\ell\gamma}(z_\ell) - \frac{2m_p^2 x^2}{Q^2} F_2 - \left( F_2 \frac{2m_p^2 x^2}{Q^2} - z^2 F_L \right) 4z_\ell(1-z_\ell) \\ + \frac{m_\ell^2 F_2}{m_\ell^2 + Q^2 z_\ell(1-z_\ell)} \left[ z P_{\gamma q}(z) - 8z_\ell(1-z_\ell) \left( 1 - z - \frac{m_p^2 x^2}{Q^2} \right) + \frac{2m_p^2 x^2}{Q^2} \right] \\ - \frac{m_\ell^2 F_L z^2}{m_\ell^2 + Q^2 z_\ell(1-z_\ell)} [2 - P_{\ell\gamma}(z_\ell)] \end{array} \right\}$$

# AP EQUATION

---

- By construction, the Lepton PDF formula is expected to satisfy a suitable Altarelli-Parisi equation.
- Taking the derivative with respect to the factorisation scale, we get

$$\frac{d}{d \ln \mu_F^2} f_\ell = \frac{\alpha(\mu_F^2)}{2\pi} P_{\ell\gamma} \otimes f_\gamma + \left( \frac{\alpha(\mu_F^2)}{2\pi} \right)^2 \sum_q P_{\ell q} \otimes f_q$$

$\alpha \times \alpha L = \alpha^2 L$                        $\alpha^2 \times \mathcal{O}(1) = \alpha^2$   
leading term                                      NLO correction

- Formally the second terms is a **NNLO QED** evolution kernel. Be aware, it should be included in DGLAP equations for the lepton pdf if NLO accuracy is required!

As a byproduct of our computation, we get an expression for the NNLO QED splitting kernel  $P_{\ell q}$  in agreement with [De Florian,Sborlini,Rodrigo, JHEP 10 (2016) 056]

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$\alpha \times \alpha L = \alpha^2 L \qquad \alpha^2 \times \mathcal{O}(1) = \alpha^2$

- Since we did not include  $\alpha^3 L^3$  terms, we miss the NLO contribution

$$\frac{\alpha(\mu_F^2)}{2\pi} P_{\ell\ell} \otimes f_\ell$$

$\alpha \times \alpha^2 L^2 = \alpha^3 L^2 \sim \alpha^2$

- We can restore its dominant contribution by solving suitable AP equations!

# CONSTRUCTION OF A FULL PDF WITH LEPTONS

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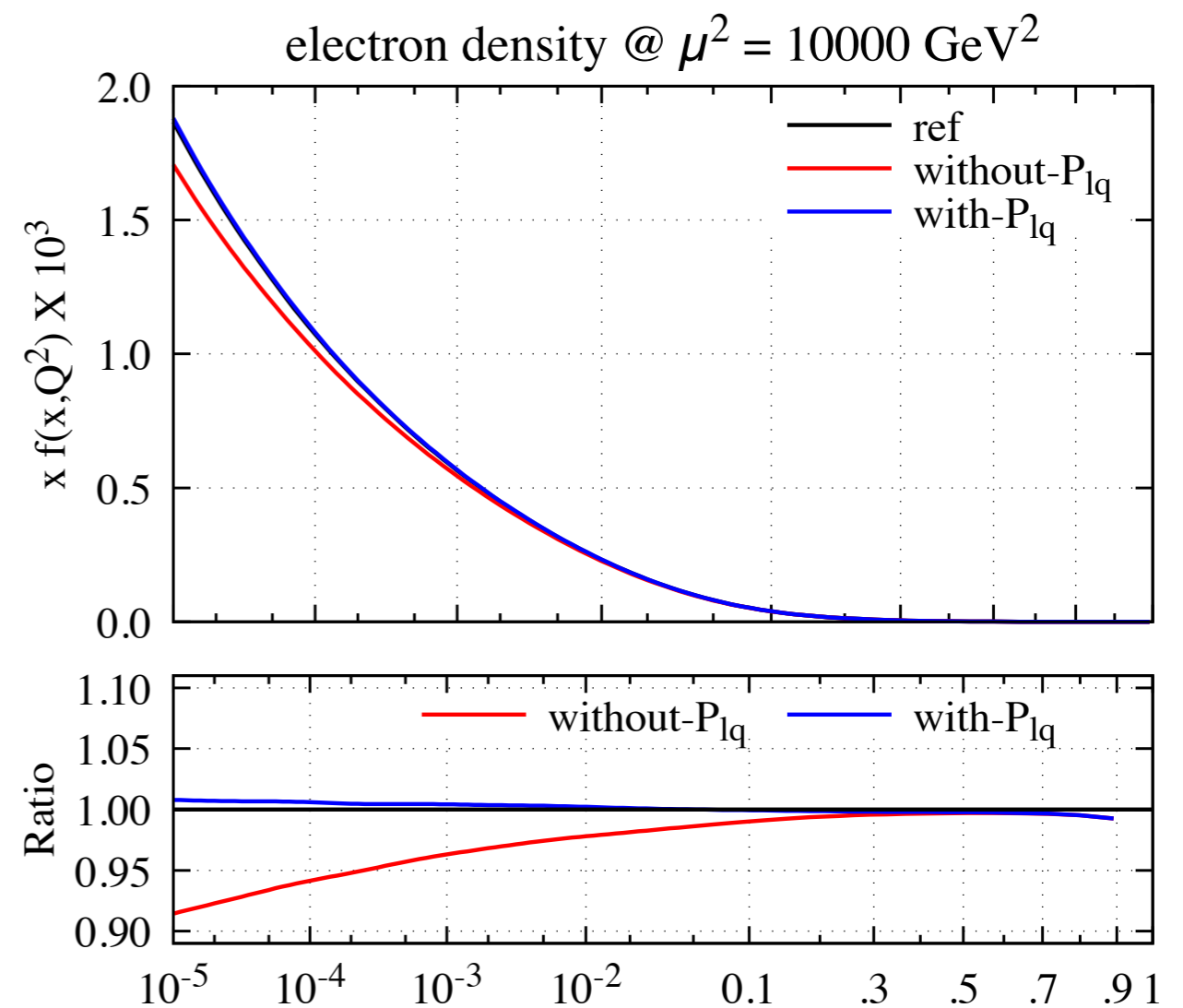
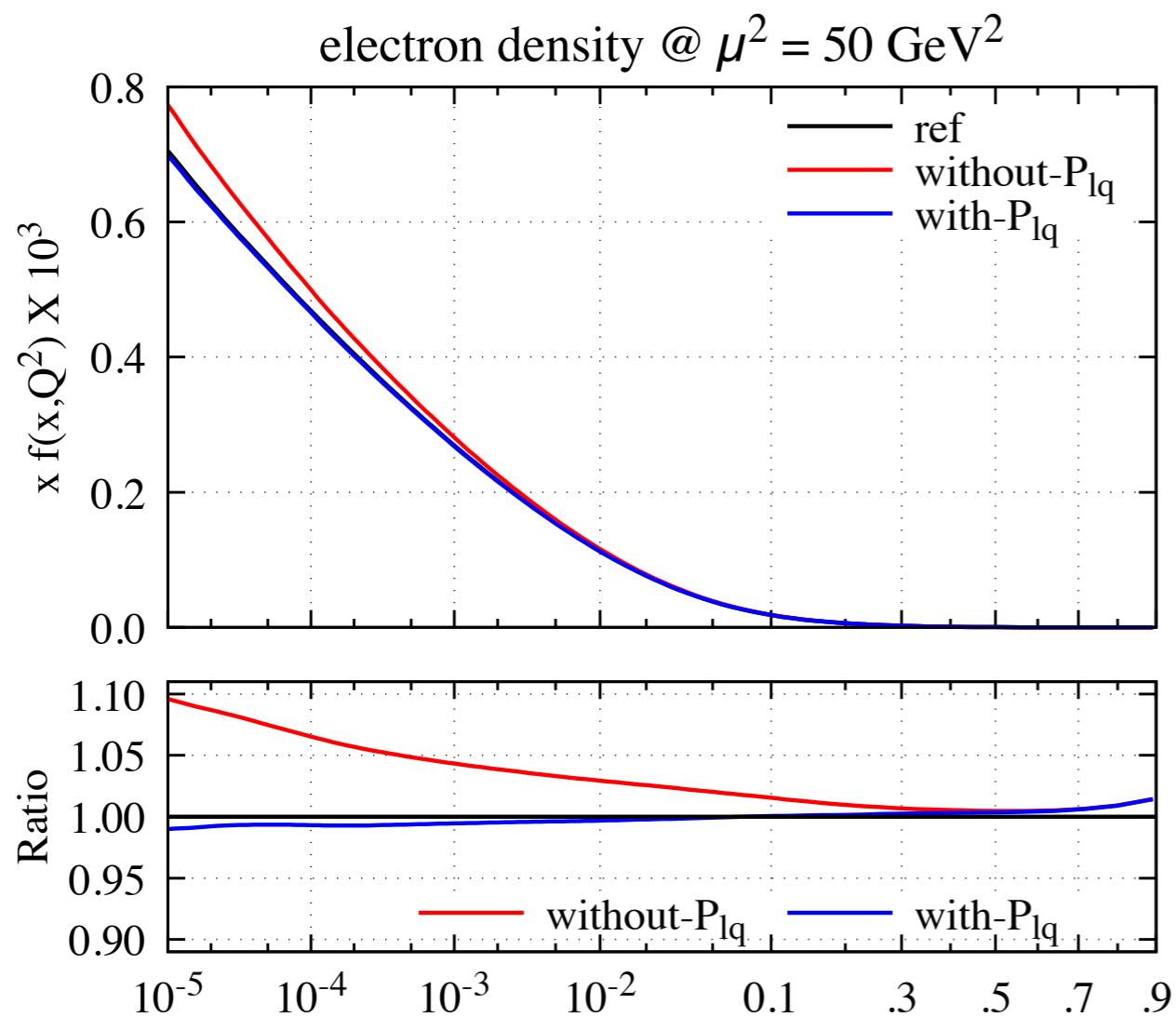
- The lepton PDF formula
  - can be computed numerically with high accuracy
  - requires experimental input for structure functions and form factors of the proton (fit + **uncertainties**) in both low- and high- $Q^2$  (from pdfs fit) regime (same data as for photon PDF)
  - allows the determination of the lepton densities at a given (**almost**) arbitrary scale. Sensitive to higher twist at low scales!
- To build a full grid, use **DGLAP** evolution (more efficient) starting from an already available pdf set! We use a input **NNPDF31\_nlo\_as\_0118\_luxqed**
  - use the lepton PDF formula to extract an initial condition for the lepton densities at a suitable reference scale ( our choice  $\mu_{\text{ref}} = 20 \text{ GeV}$  )
  - solve the integro-differential DGLAP equations including all the relevant splitting kernels which contribute to the desired target accuracy:

$$\alpha_s, \quad \alpha_s \alpha, \quad \alpha^2 \text{ (} P_{\ell q} \text{ must be included!)}$$

- make available the grid in a standard format (aka LHAPDF)

# IMPORTANCE of the $\mathcal{O}(\alpha^2) P_{\ell q}$ -SPLITTING in DGLAP

- If not included, it leads to  $\mathcal{O}(10\%)$  differences in the small-x region, where its contribution is logarithmic enhanced





# UNCERTAINTIES on LEPTON DENSITIES

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We consider

- 6 variations on the fits used as input data for the proton structure functions and form factor (as in the photon PDF papers)
- a scale variation prescription to estimate the uncertainty due to missing higher orders
- replicas to take into account PDF uncertainties

**Procedure:** for each replica member  $m$  in the original NNPDF set

1. we apply our method to add leptons
2. we compute the correction

$$\Delta_i^{(m)}(x, \mu_F) = \sum_{j=1}^7 \frac{f_{i,(j)}^{(0)}(x, \mu_F) - f_i^{(0)}(x, \mu_F)}{f_i^{(0)}(x, \mu_F)} f_i^{(m)}(x, \mu_F) \times R(m, j)$$

7 variations of the central set

Gaussian distributed random number with unit variance

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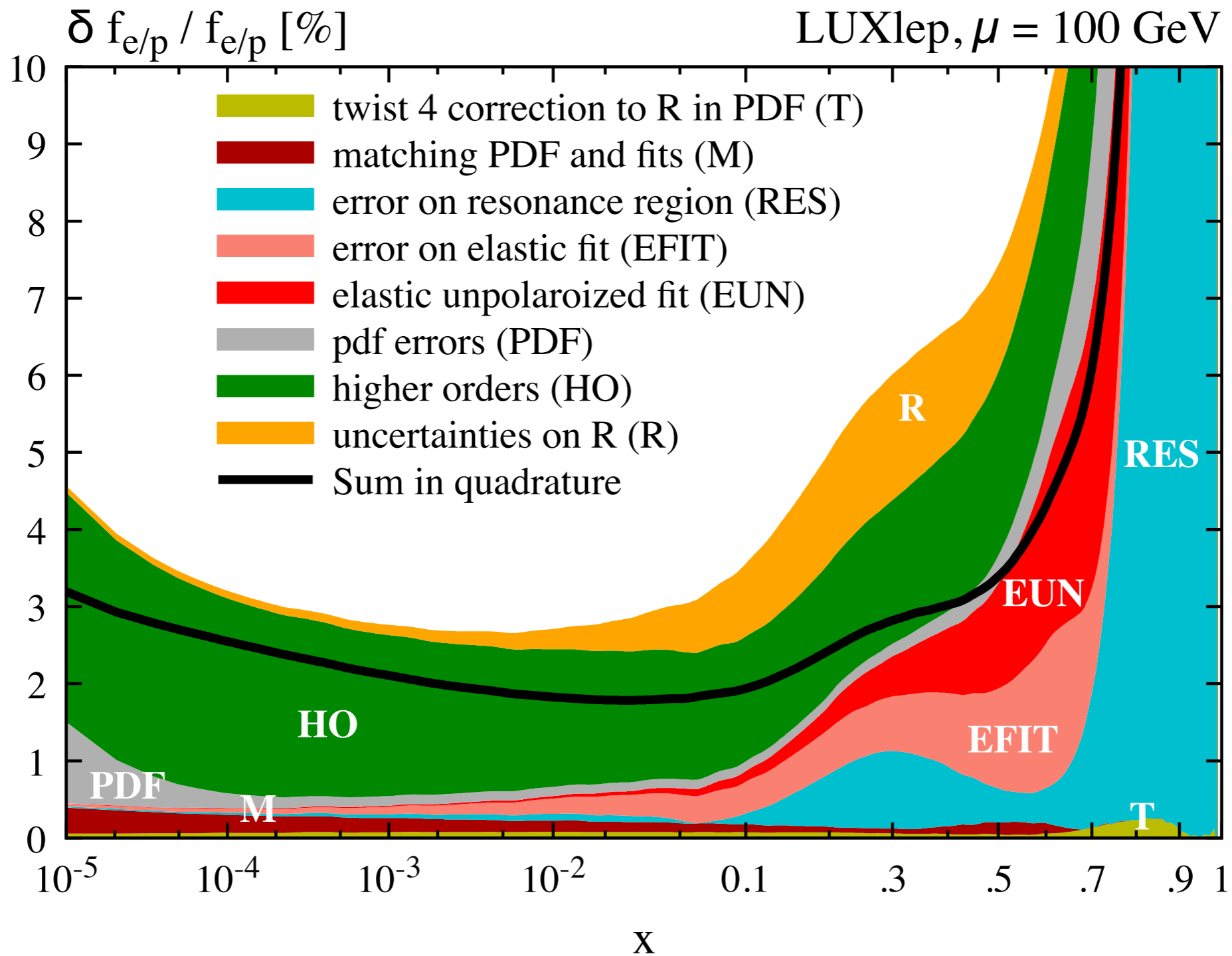
**Procedure:** for each replica member  $m$  in the original NNPDF set

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2. we compute the correction
3. we correct the replicas as

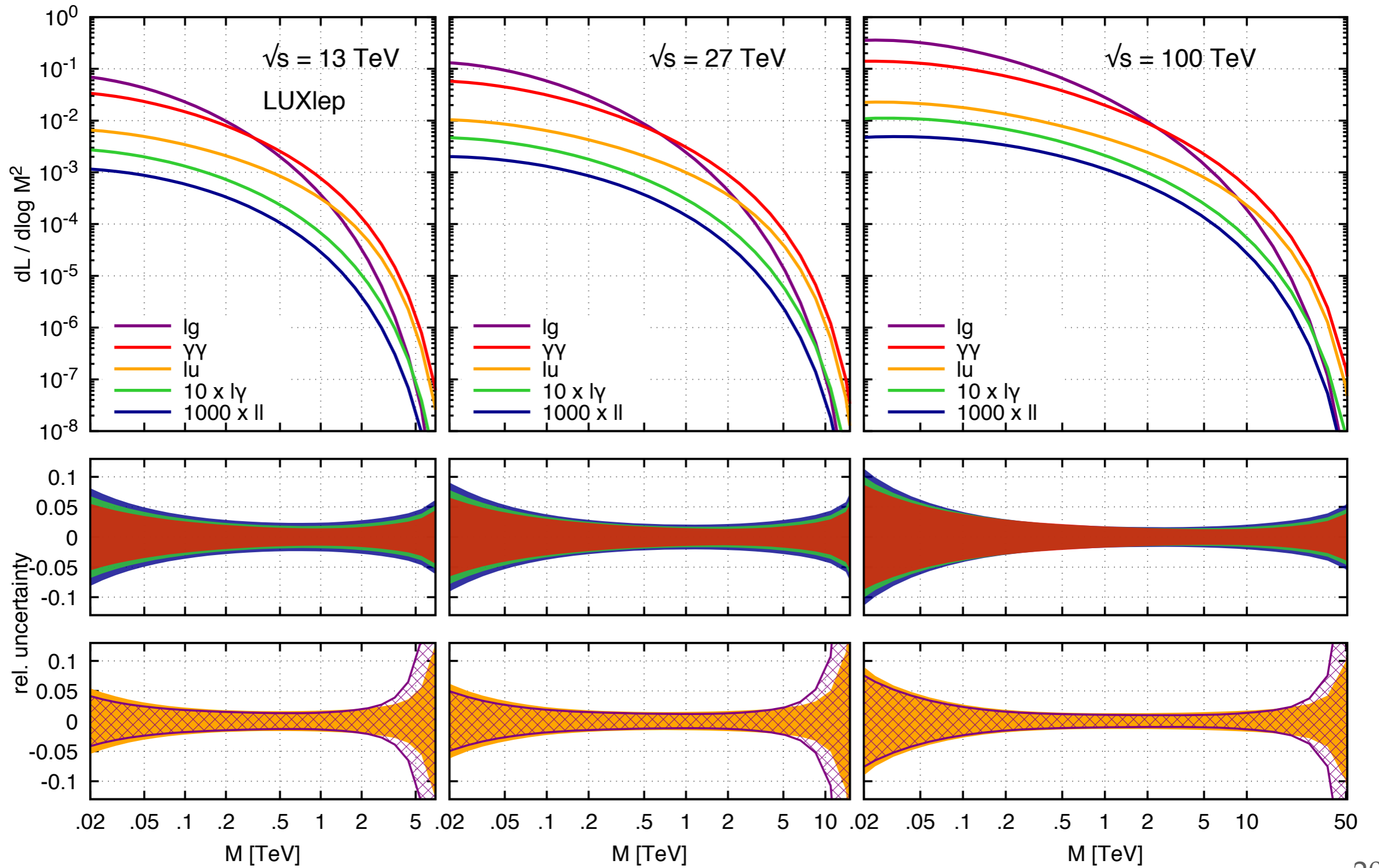
$$f_i^{(m)}(x, \mu_F) \rightarrow f_i^{(m)}(x, \mu_F) + \Delta_i^{(m)}(x, \mu_F) - \frac{1}{N_{rep}} \sum_{k=1}^{N_{rep}} \Delta_k^{(m)}(x, \mu_F)$$

so that the average of all replicas is not shifted.

# UNCERTAINTIES on LEPTON DENSITIES



# LUMINOSITIES



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# LHC PHENOMENOLOGY

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# SM LEPTON-LEPTON SCATTERING

- Lepton densities are **very small**, but lepton-lepton processes might be observed. Consider different flavours / same sign combination

$$p_{T,\ell} > 20 \text{ GeV}, \quad |\eta| < 2.4$$

	$e^+ \mu^-$	$e^+ \tau^-$	$\mu^+ \tau^-$	$e^+ e^+$	$\mu^+ \mu^+$	$\tau^+ \tau^+$
$\sigma_{13\text{TeV}}$ [fb]	$0.29^{+0.13}_{-0.10}$	$0.18^{+0.11}_{-0.08}$	$0.16^{+0.10}_{-0.07}$	$0.24^{+0.10}_{-0.08}$	$0.19^{+0.09}_{-0.07}$	$0.08^{+0.06}_{-0.04}$
$\sigma_{27\text{TeV}}$ [fb]	$0.53^{+0.25}_{-0.18}$	$0.34^{+0.21}_{-0.15}$	$0.30^{+0.19}_{-0.14}$	$0.440^{+0.19}_{-0.14}$	$0.34^{+0.16}_{-0.12}$	$0.14^{+0.12}_{-0.07}$

- We considered only WW background and we found it is negligible after requiring suitable **signal-like cuts**. Heavy flavour production background might be relevant

- A dedicated analysis **requires Shower Monte Carlo programs** for lepton initiated processes
- Theoretical uncertainty dominated by factorisation scale variation. “NLO” corrections should be included

**REMARKS**

# SM LEPTON-LEPTON SCATTERING

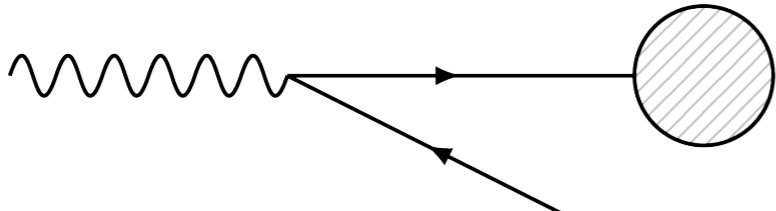
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## 1. Parton Shower

- Hardest radiation accompanying an initial state lepton **is another lepton**
- **Reduced hadronic activity** in the event
- So far, no Parton Shower program handle (backward) initial state shower originated by leptons
- Peter Richardson provided us a patch for Herwig. Analysis are on going

## 2. "NLO" corrections

- What do we mean by "NLO"? There are not any coloured particles
- To match the NLO accuracy of the LeptonPDF computation, photon induced corrections must be added



The diagram shows a wavy line representing a photon on the left. It splits into two paths: one is a solid line representing a lepton that continues to the right and ends in a shaded circle, and the other is a solid line representing a photon that branches off downwards and to the right.

$$\Rightarrow \frac{[f_\gamma] \times \alpha}{[f_\ell]} = \frac{\alpha^2 L}{\alpha^2 L^2} = \frac{1}{L} \approx \alpha_s$$

# SM LEPTON-LEPTON SCATTERING

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- **Reduced hadronic activity** in the event
- So far, no Parton Shower program handle (backward) initial state shower originated by leptons
- Peter Richardson provided us a patch for Herwig. Analysis are on going

## 2. "NLO" corrections

- What do we mean by "NLO"? There are not any coloured particles
- To match the NLO accuracy of the LeptonPDF computation, photon induced corrections must be added

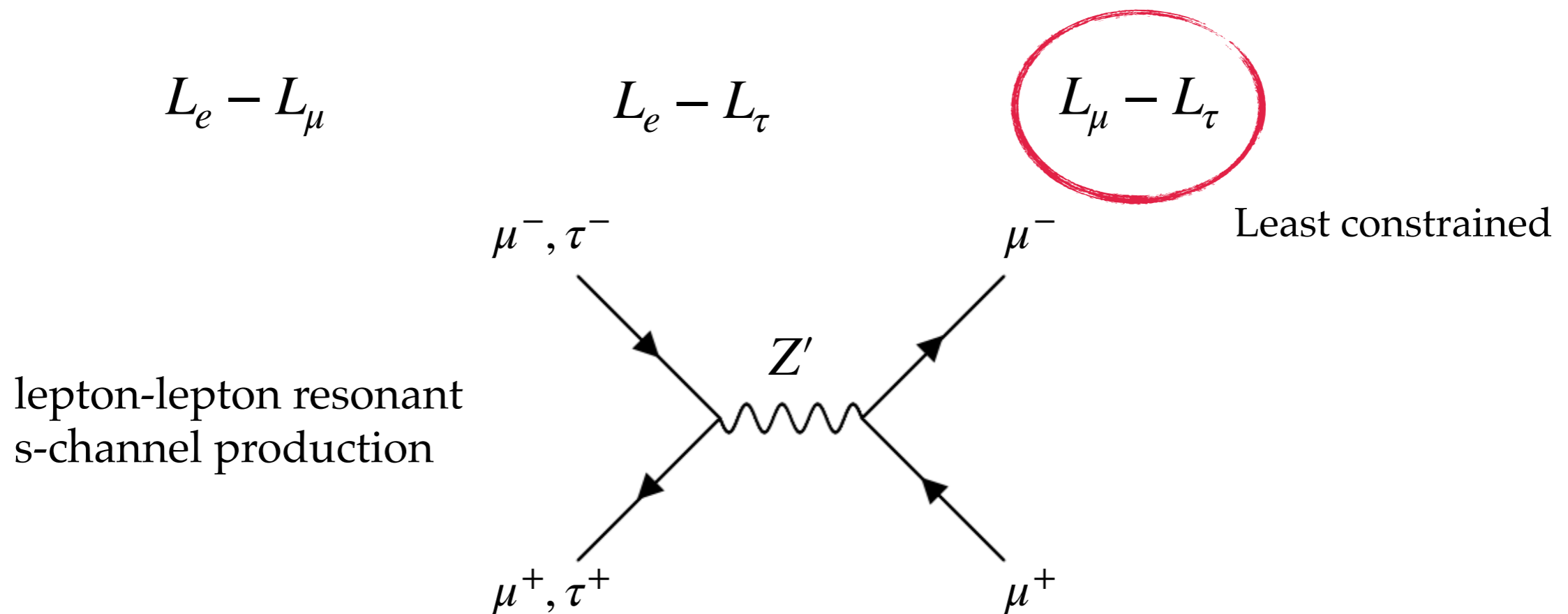


NLO+PS within the reach!



# BSM searches: $L_\mu - L_\tau$ $Z'$ boson

- One of the simplest idea is to look for new “hadro-phobic” gauge forces
- A minimal extension of the SM is provided by gauging **anomaly-free** combinations of family leptons numbers [[He, Joshi, Lew, Volkas, PRD 44 \(1991 2118\)](#)]:



- **Analysis:** bump search in the di-muon invariant mass spectrum

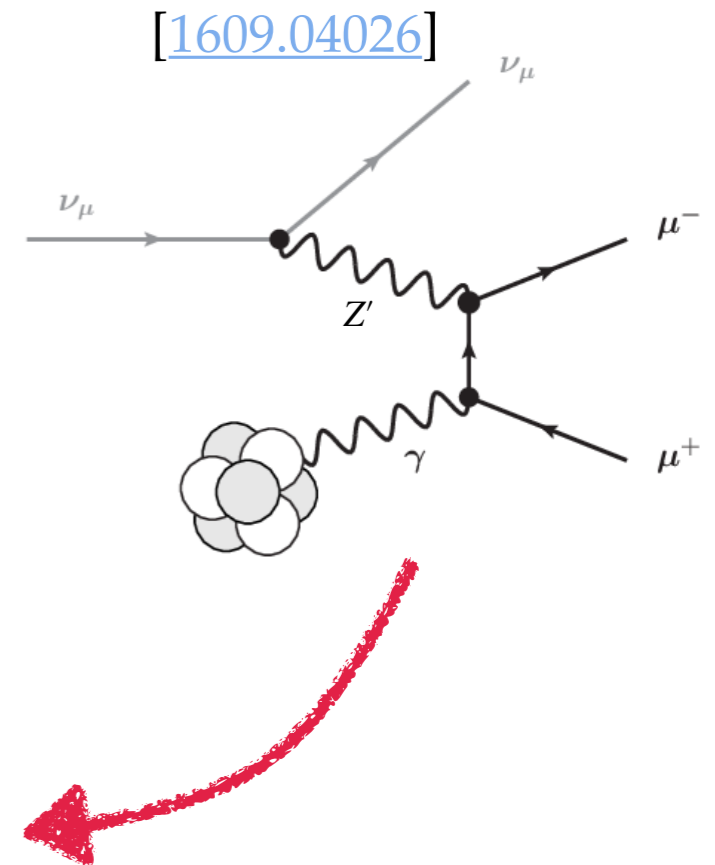
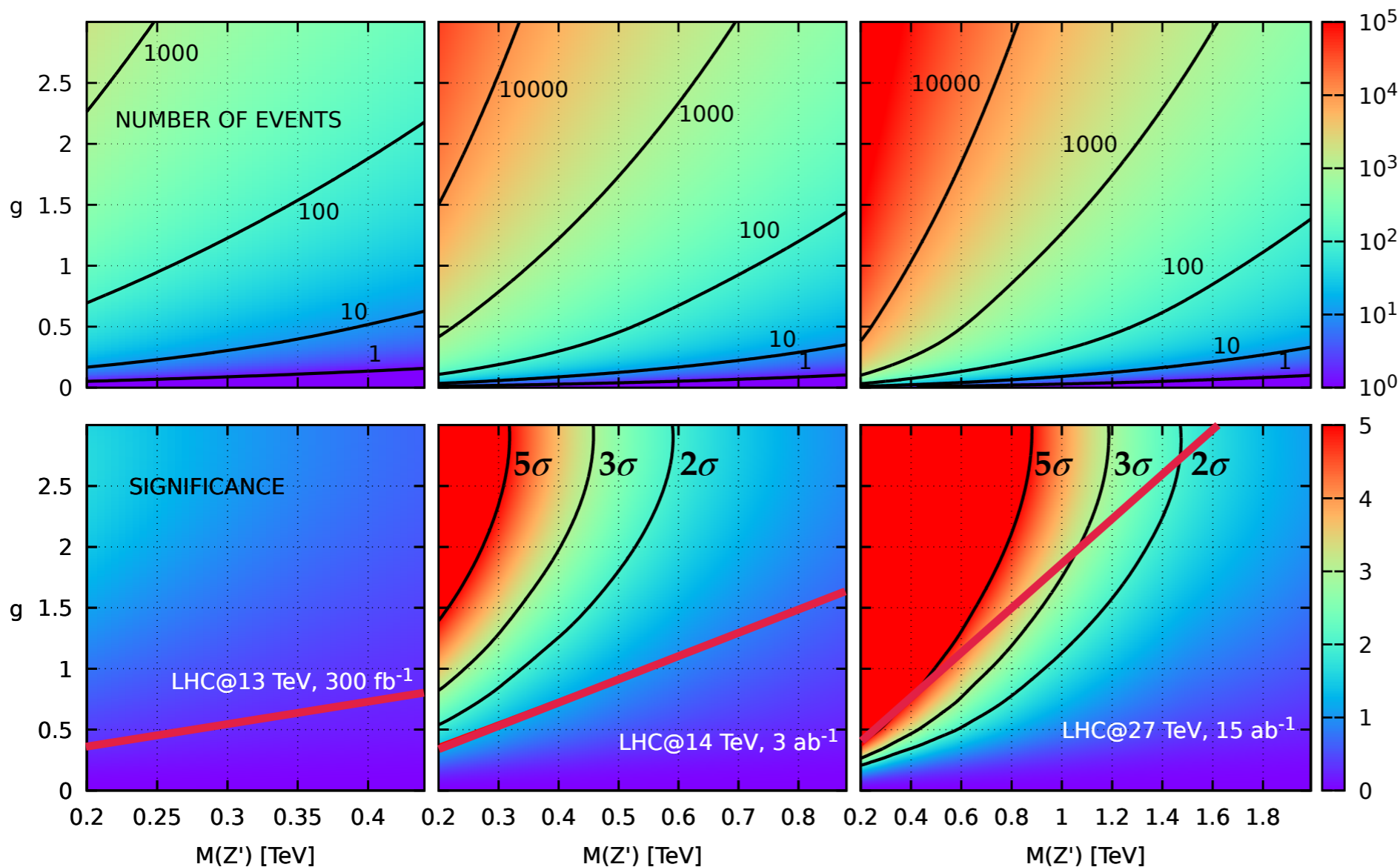
$$b_w = \sqrt{\Gamma_{Z'}^2 + r^2 M_{Z'}^2}, \quad \Gamma_{Z'} = \frac{g}{4\pi} M_{Z'}$$

reconstruction efficiency from [[1812.10529](#)]  
 $r$ :  $\mu$  energy resolution from [[1804.04528](#)]

- **Background:** di-muon Drell-Yan production

# BSM searches: $L_\mu - L_\tau$ $Z'$ boson

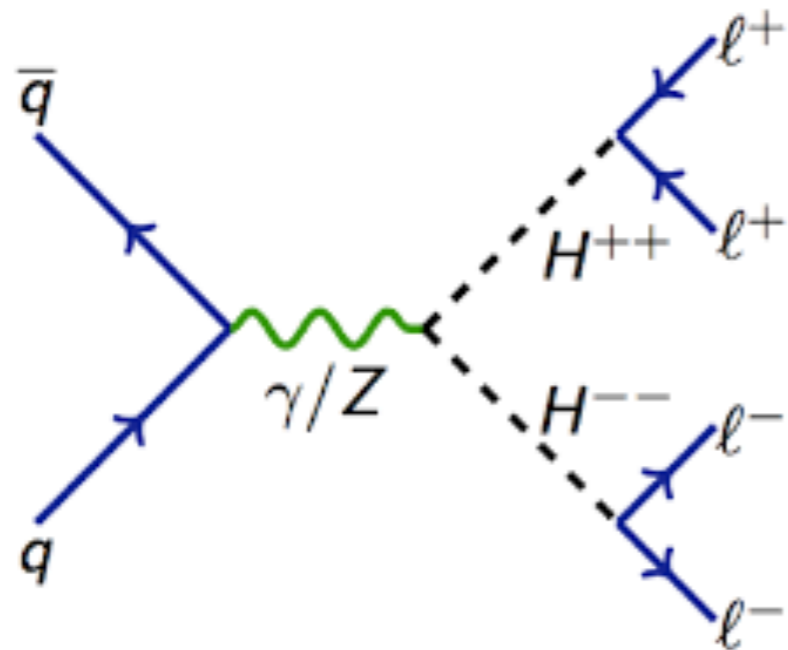
- Direct LHC limits **weaker** than indirect constraints from **neutrino trident** (low energy physics constraint). Need HE-LHC upgrade to make them comparable in strength
- **Hadronic activity** may play a role to reduce the Drell-Yan background



# BSM searches: doubly charged Higgs $H^{\pm\pm}$

- Look for BSM processes with (almost) **background free**
- Example: **doubly charged Higgs** (mainly occurring in extensions of the SM which aim to accommodate neutrino masses)
- $H^{\pm\pm}$  couples to leptons and  $W$  bosons. We assume a typical scenario in which the coupling to  $W$  bosons is negligible

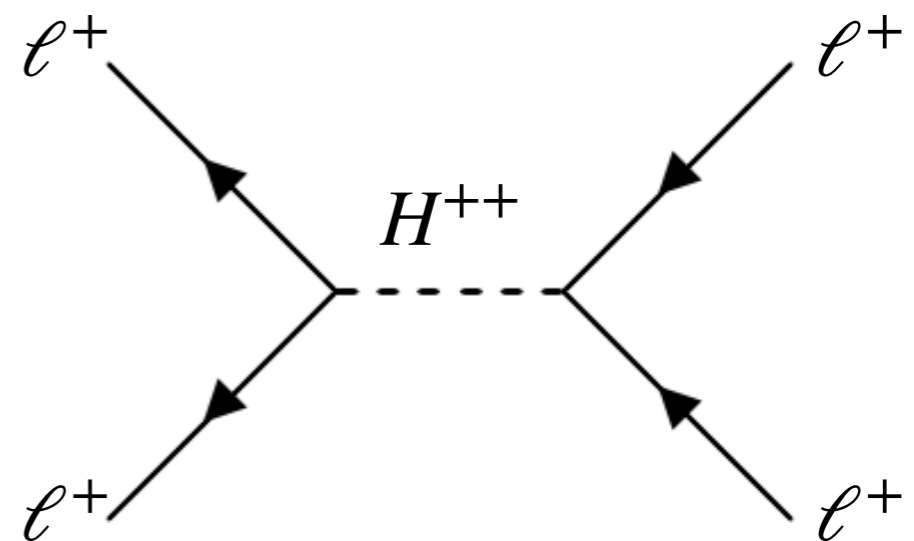
## Pair Production



ATLAS [[1710.09748](#)]

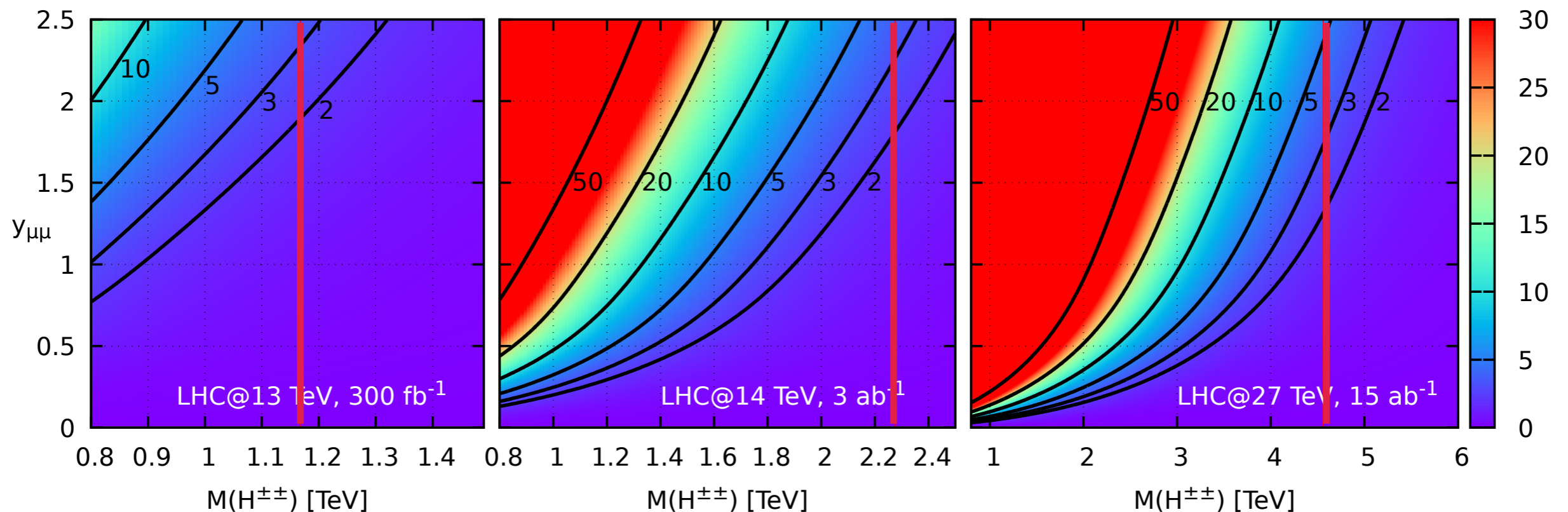
CMS [[1902.04773](#)]

## Single resonant production



# BSM searches: doubly charged Higgs $H^{\pm\pm}$

- We assumed **background free** and minimal coupling to one lepton species
- For sufficiently **large** Yukawa  $y_{\mu\mu}$  coupling s-channel production for a doubly charged Higgs **may have a mass reach comparable** to analyses relying upon pair production



Pair Production projection taken from *de Melo et al* [[1909.07429](#)]

# REMARKS - "take home message"

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Proton can be seen as broad band beams of leptons

- this gives access to **single resonant production** of new states which **preferably** couple to leptons
- sensitivity to coupling ( complementarity to pair production )

Lepton densities are in fact small but handful events can be produced. Ideal situations:

- **large enough couplings**
- rare SM events / signatures to be (almost) **background free**

So far we consider lepton-lepton processes

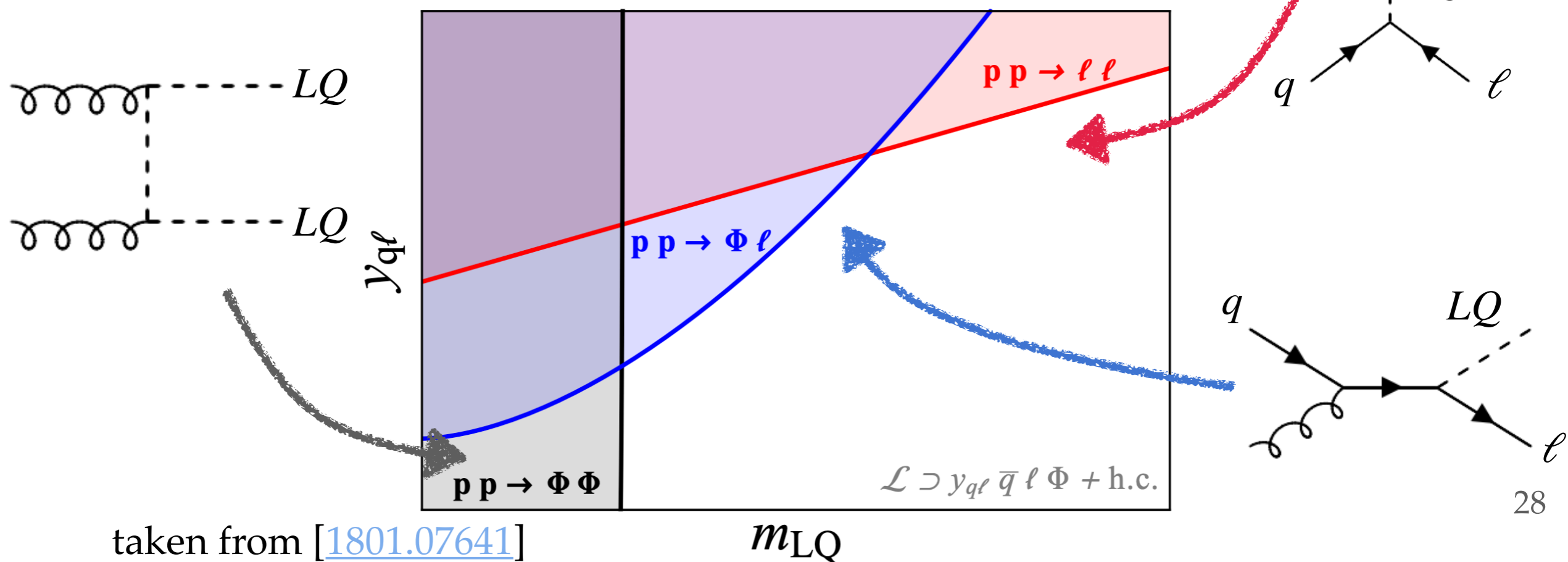
- in lepton-quark collisions only one lepton PDF suppression!
- ideal BSM candidate: **LeptoQuark** searches in single resonant channel

# LeptoQuarks Searches at LHC: INTRO

LeptoQuark appear in several extensions of the Standard Model, and are advocated as a possible explanation of the flavour anomalies (for a recent review *Dorsner et al* [[1603.04993](#)])

At LHC, the searches focus on three production mechanisms

- Pair Production (PP)
- Single Production (SP) associated with a lepton
- Drell-Yan like Production (DY)



# LeptoQuarks Searches at LHC: STATUS

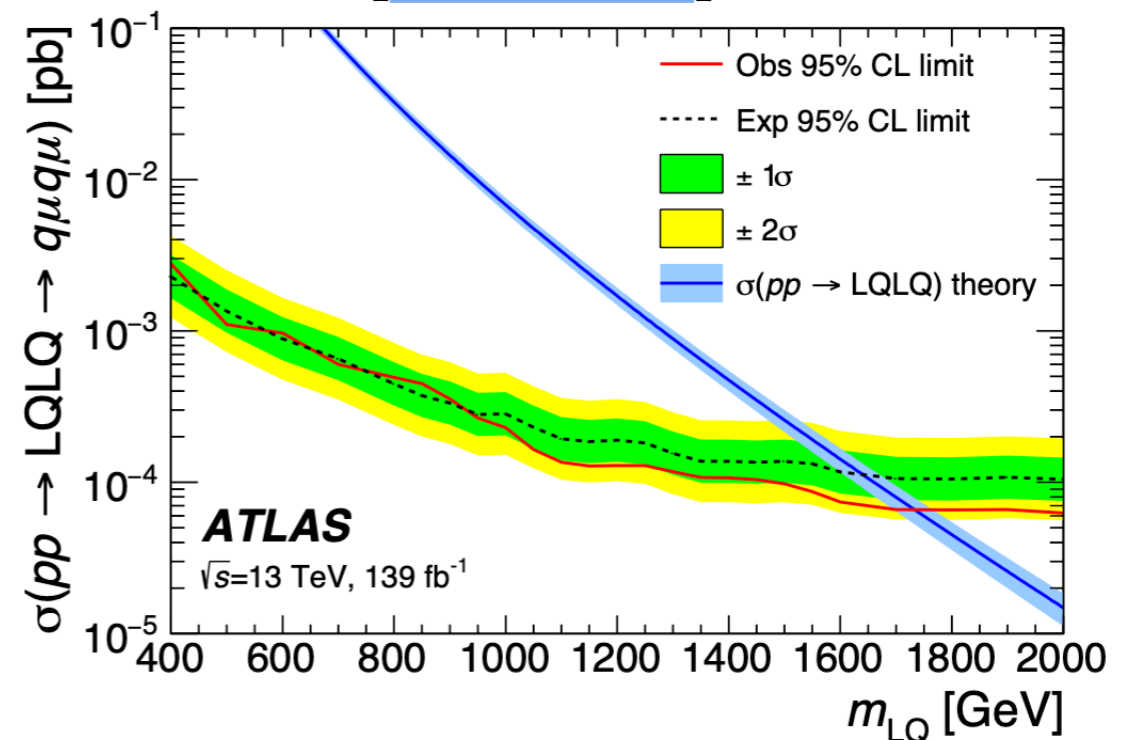
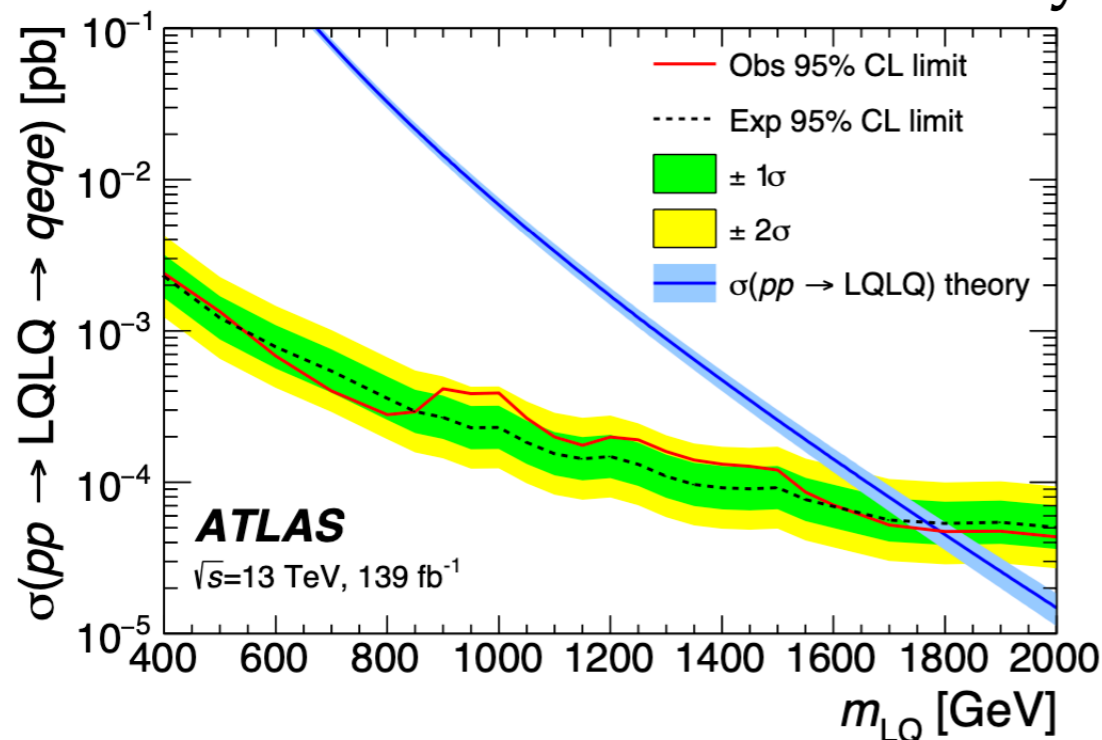
<b>LQ</b>	Scalar LQ 1 <sup>st</sup> gen	LQ mass	1.4 TeV	1902.00377
	Scalar LQ 2 <sup>nd</sup> gen	LQ mass	1.56 TeV	1902.00377
	Scalar LQ 3 <sup>rd</sup> gen	$LQ_3^u$ mass	1.03 TeV	1902.08103
	Scalar LQ 3 <sup>rd</sup> gen	$LQ_3^d$ mass	970 GeV	1902.08103

ATLAS Exotics Searches

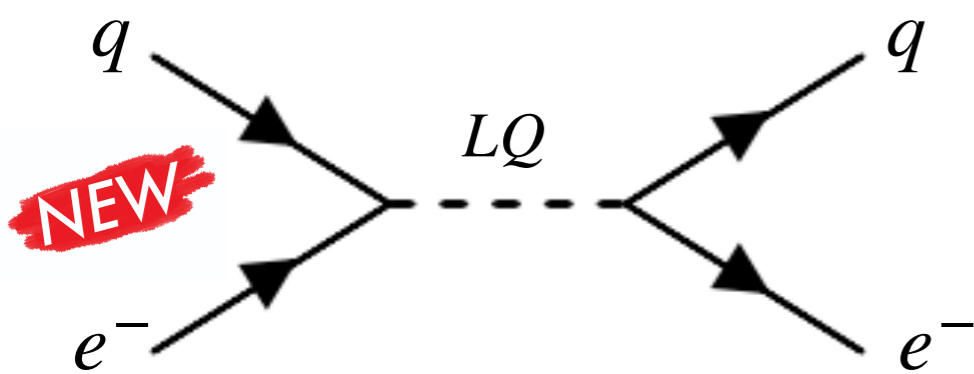
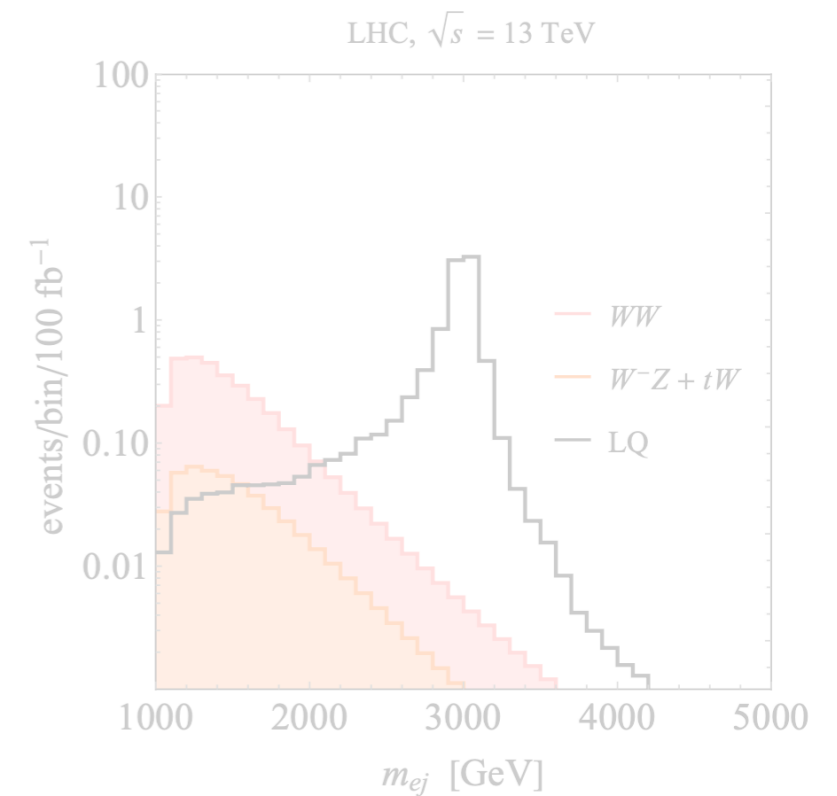
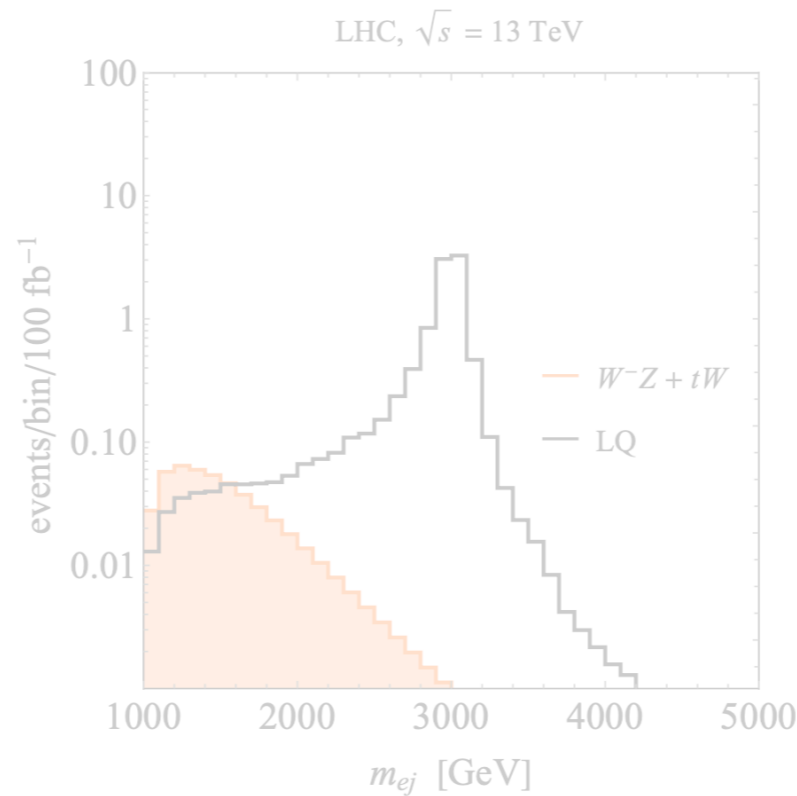
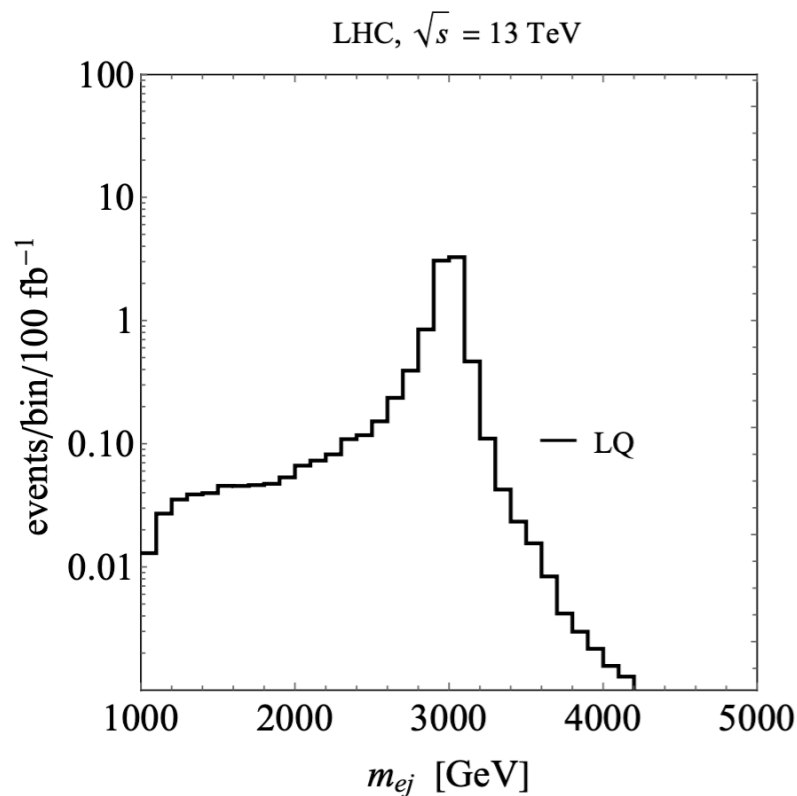
<b>Leptoquarks</b>	scalar LQ (pair prod.), coupling to 1 <sup>st</sup> gen. fermions, $\beta = 1$	$<1.44$	1811.01197 ( $2e + 2j$ )	36 fb <sup>-1</sup>
	scalar LQ (pair prod.), coupling to 1 <sup>st</sup> gen. fermions, $\beta = 0.5$	$<1.27$	1811.01197 ( $2e + 2j; e + 2j + E_T^{\text{miss}}$ )	36 fb <sup>-1</sup>
	scalar LQ (pair prod.), coupling to 2 <sup>nd</sup> gen. fermions, $\beta = 1$	$<1.53$	1808.05082 ( $2\mu + 2j$ )	36 fb <sup>-1</sup>
	scalar LQ (pair prod.), coupling to 2 <sup>nd</sup> gen. fermions, $\beta = 1$	0.8–1.5	1811.10151 ( $1\mu + 1j + E_T^{\text{miss}}$ )	77 fb <sup>-1</sup>
	scalar LQ (pair prod.), coupling to 2 <sup>nd</sup> gen. fermions, $\beta = 0.5$	$<1.29$	1808.05082 ( $2\mu + 2j; \mu + 2j + E_T^{\text{miss}}$ )	36 fb <sup>-1</sup>
	scalar LQ (pair prod.), coupling to 3 <sup>rd</sup> gen. fermions, $\beta = 1$	$<1.02$	1811.00806 ( $2\tau + 2j$ )	36 fb <sup>-1</sup>
	scalar LQ (single prod.), coup. to 3 <sup>rd</sup> gen. ferm., $\beta = 1, \lambda = 1$	$<0.74$	1806.03472 ( $2\tau + b$ )	36 fb <sup>-1</sup>

CMS EXO results

## First Full Run II analysis from ATLAS [2006.05872]



# LeptoQuarks Searches at LHC: s-channel production



Minimal scalar LeptoQuark which couples to  $e^-$  and u quark

Benchmark point:  $M_{LQ} = 3$  TeV,  $\lambda_{eu} = 1$

Simulated at LO+PS

To target signal

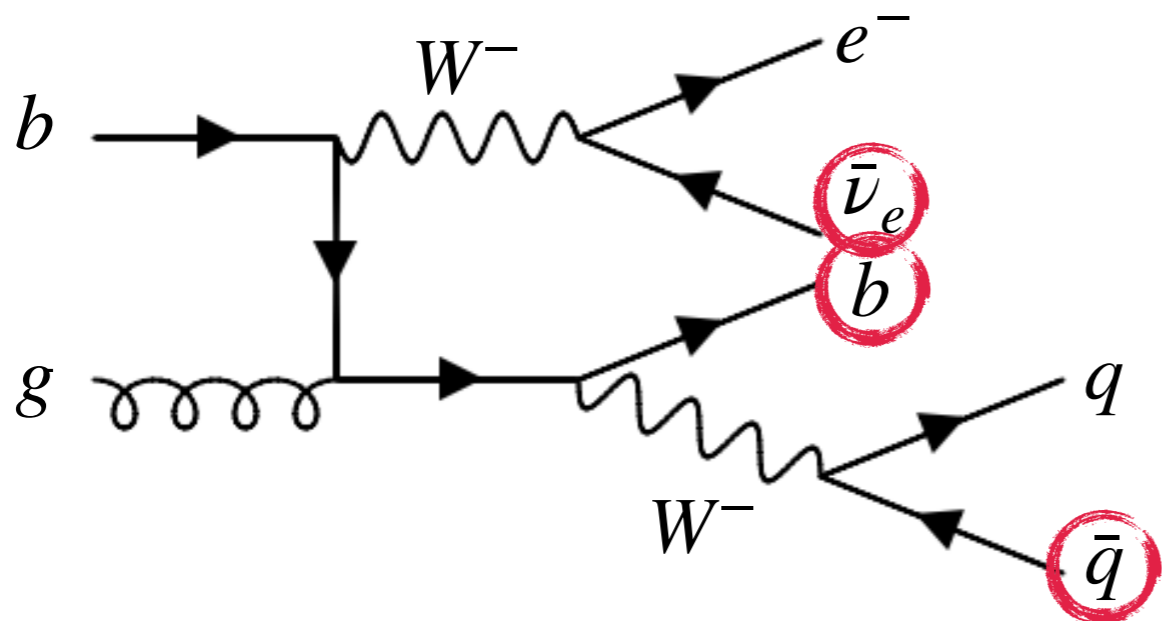
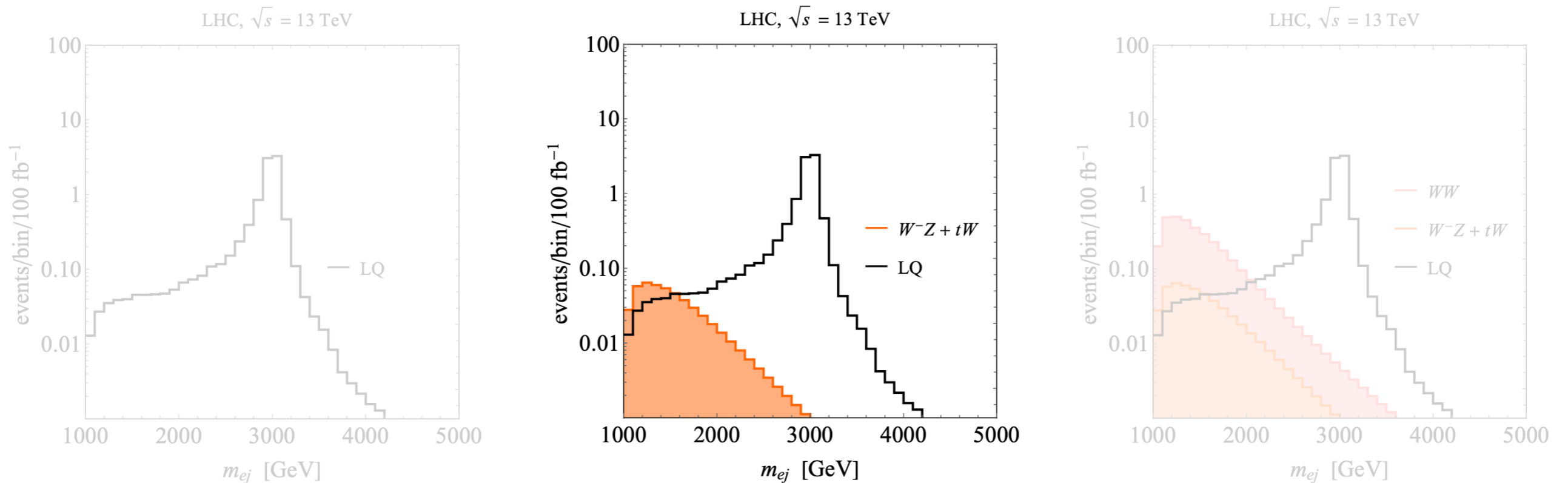
$$|\eta_{\ell_1}| < 2.5, \quad p_{T,\ell_1} > 500 \text{ GeV}, \quad |\eta_{j_1}| < 2.5, \quad p_{T,j_1} > 500 \text{ GeV}$$

Suppress background: cut on missing energy, veto on extra leptons and jets

$$E_{T,\text{miss}} < 50 \text{ GeV}, \quad |\eta_{\ell_2}| < 2.5, \quad p_{T,\ell_2} > 7 \text{ GeV}, \quad |\eta_{j_2}| < 2.5, \quad p_{T,j_2} > 30 \text{ GeV}$$



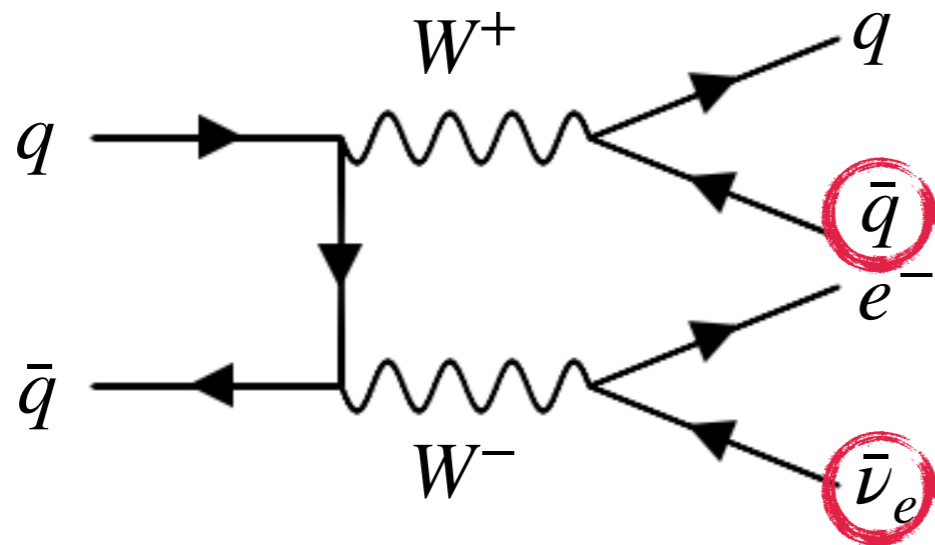
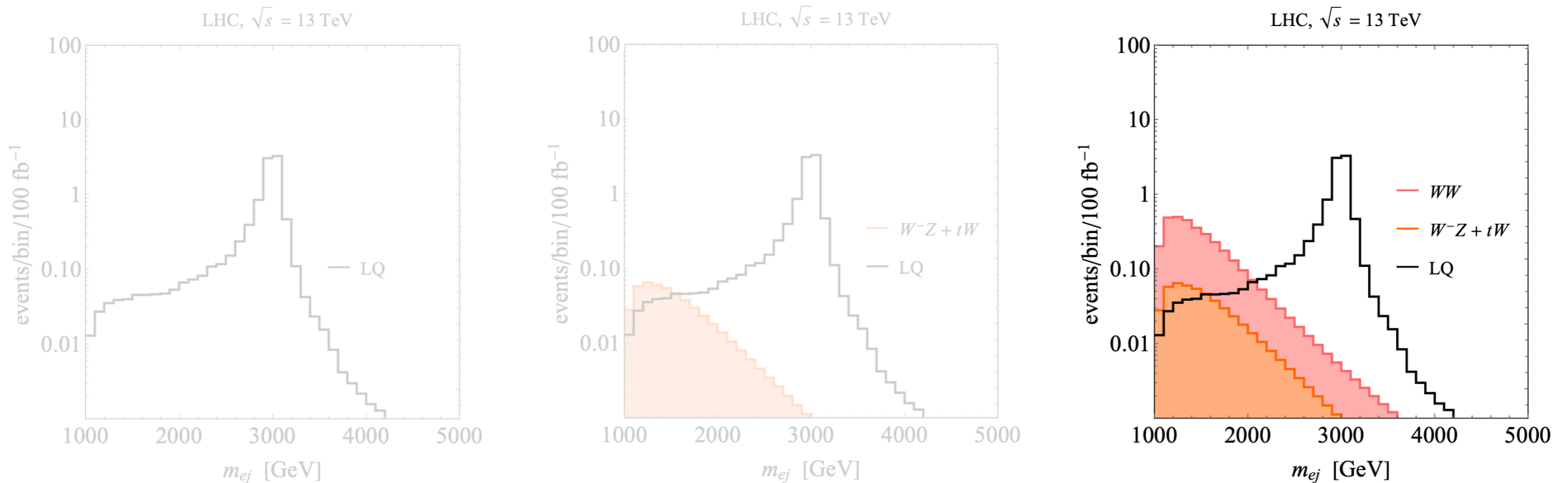
# LeptoQuarks Searches at LHC: s-channel production



Simulated at LO+PS and normalised to the NLO QCD result

Suppressed by  $E_T$  miss & jet veto requirements

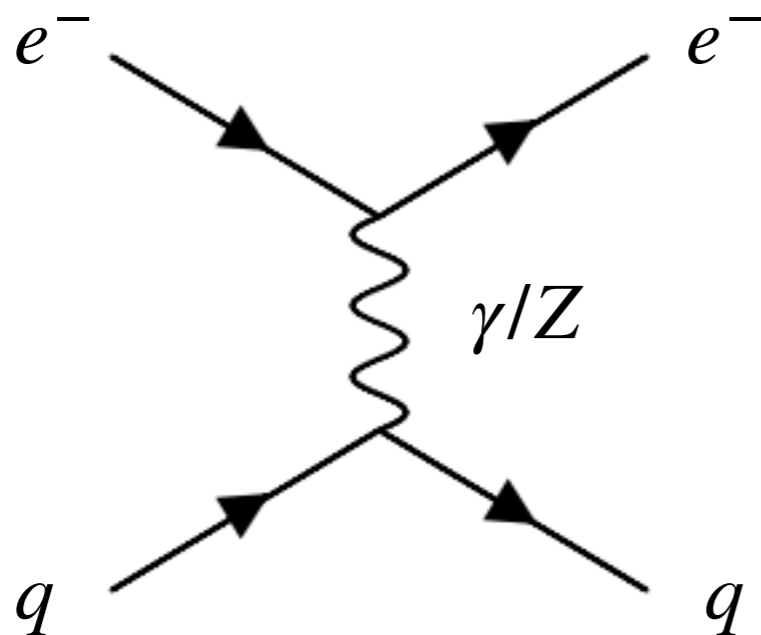
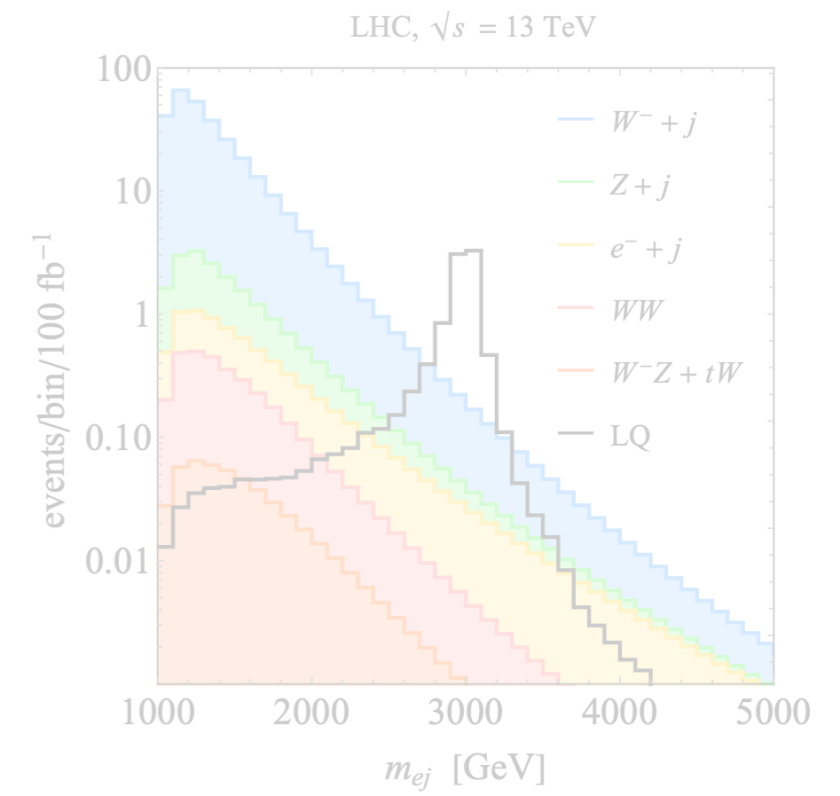
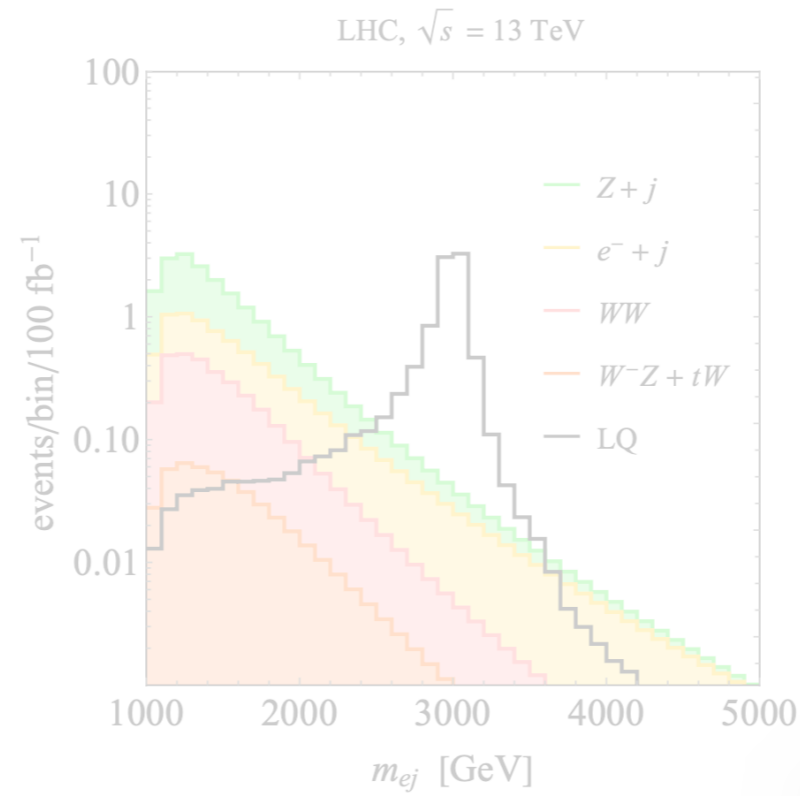
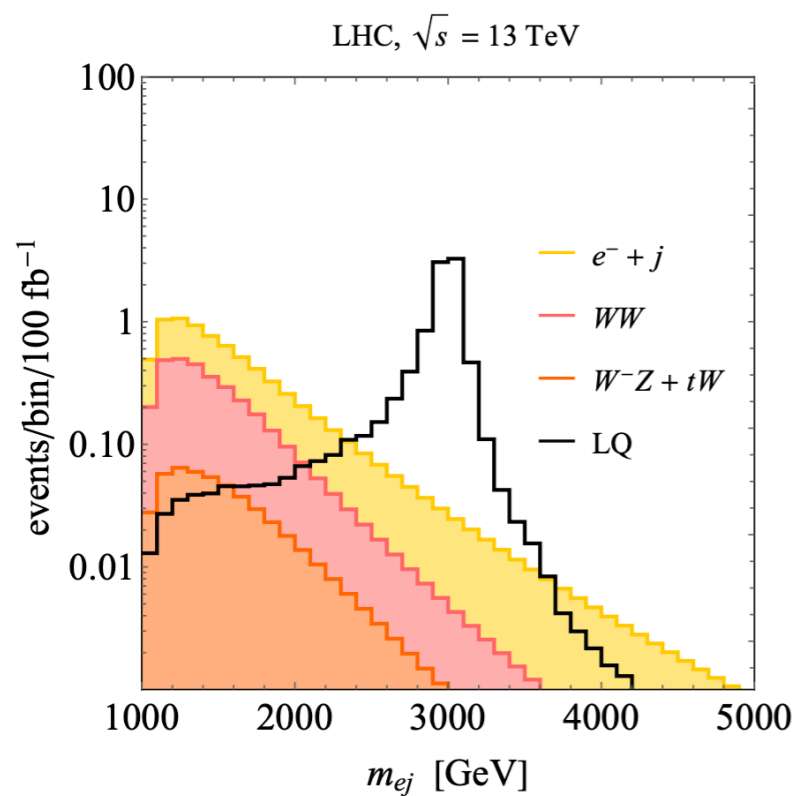
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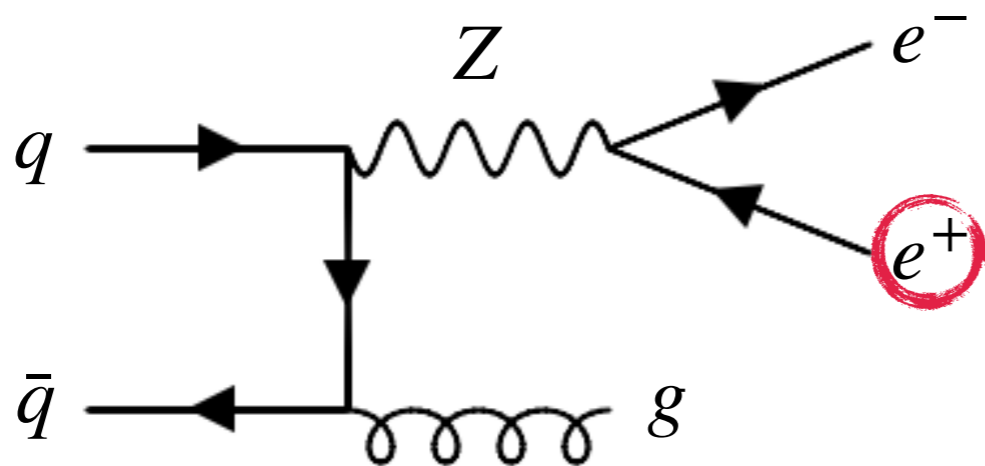
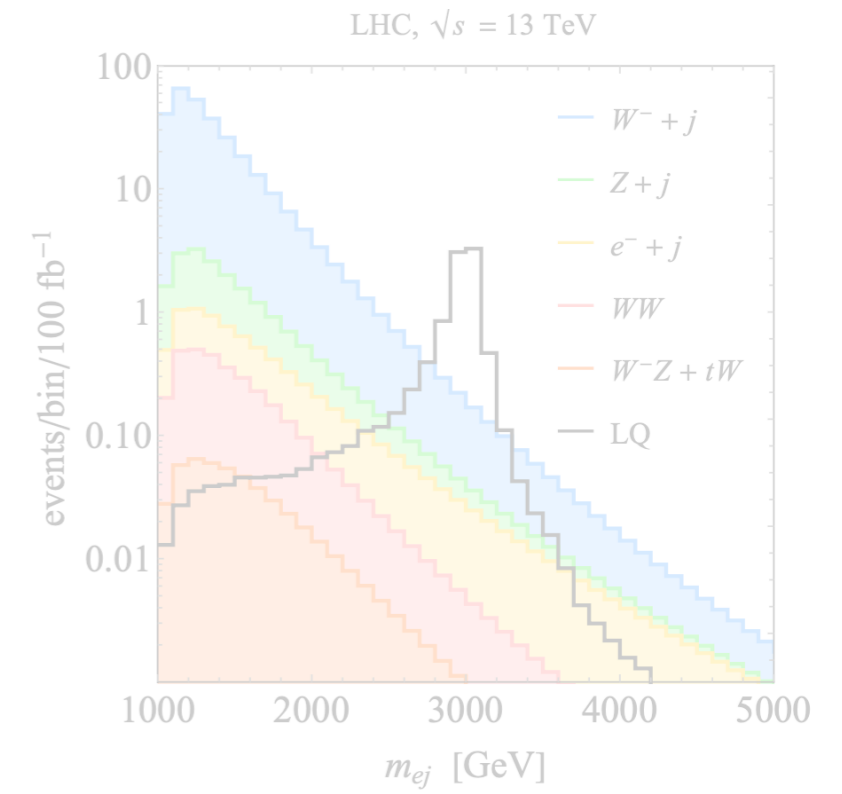
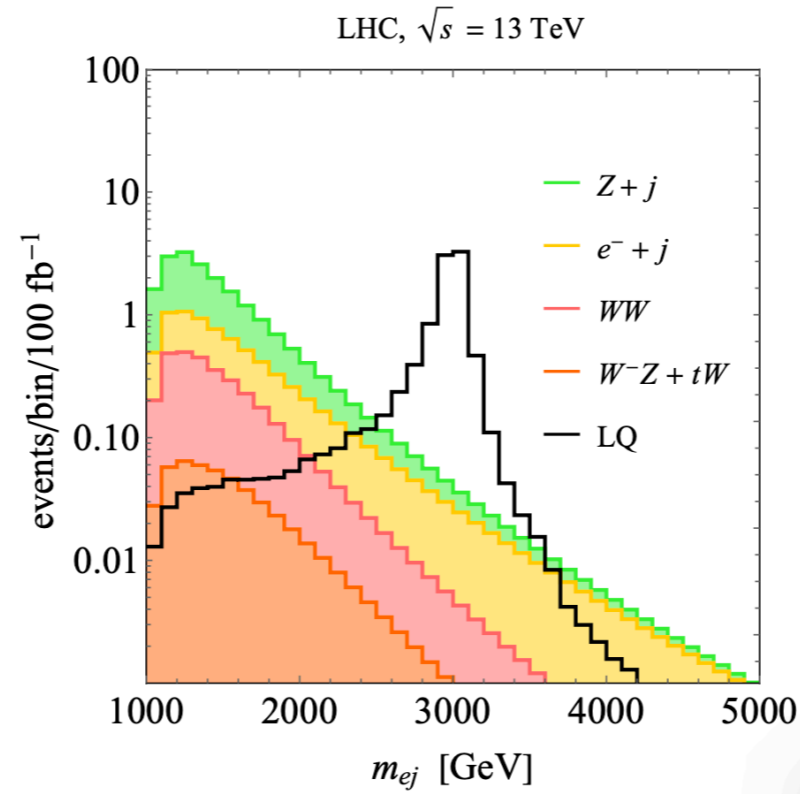
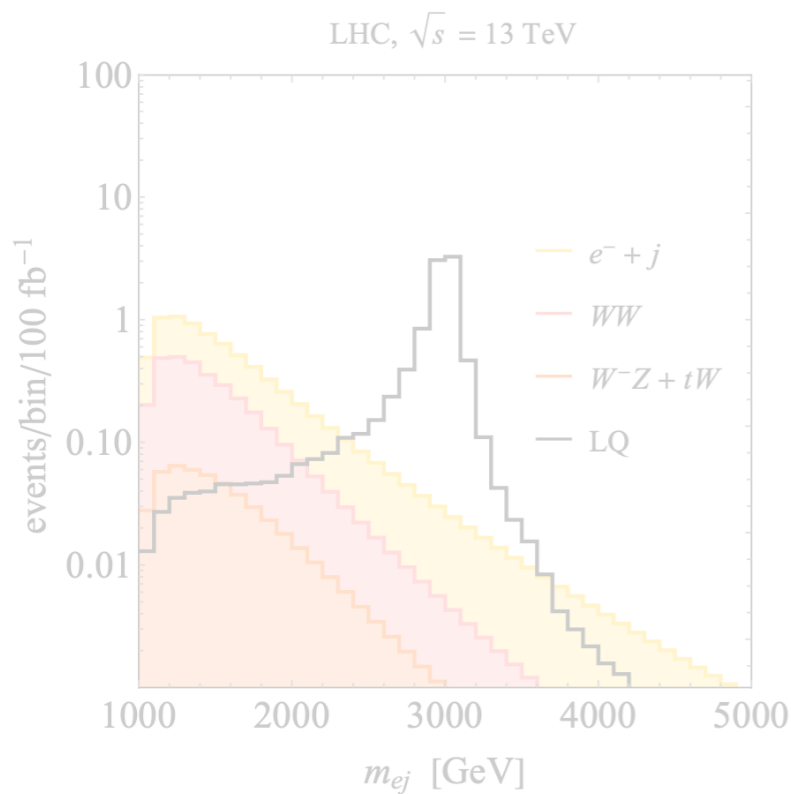
# LeptoQuarks Searches at LHC: s-channel production



Irreducible background.  
Simulated at LO+PS

Relevant at high-invariant  
lepton-jet mass

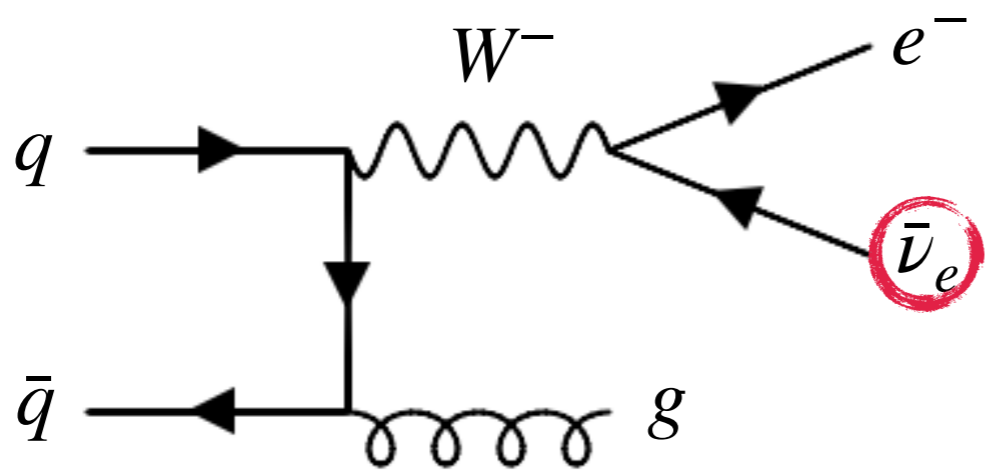
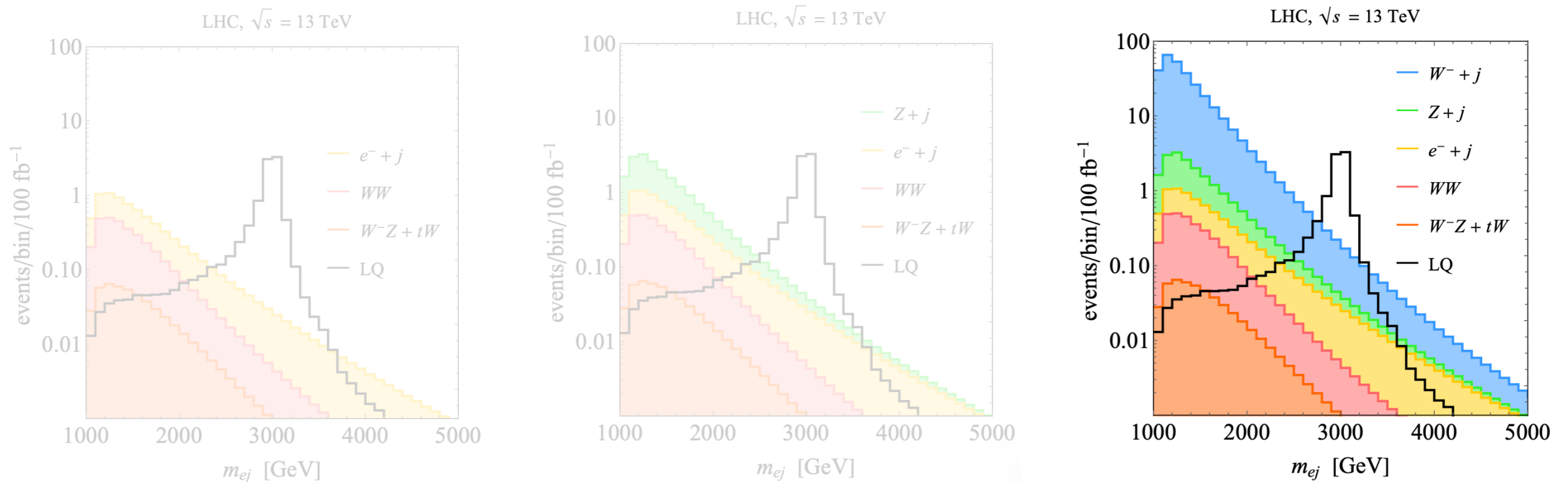
# LeptoQuarks Searches at LHC: s-channel production



Simulated at LO+PS and normalised to the NLO QCD result

Suppressed by lepton veto requirement

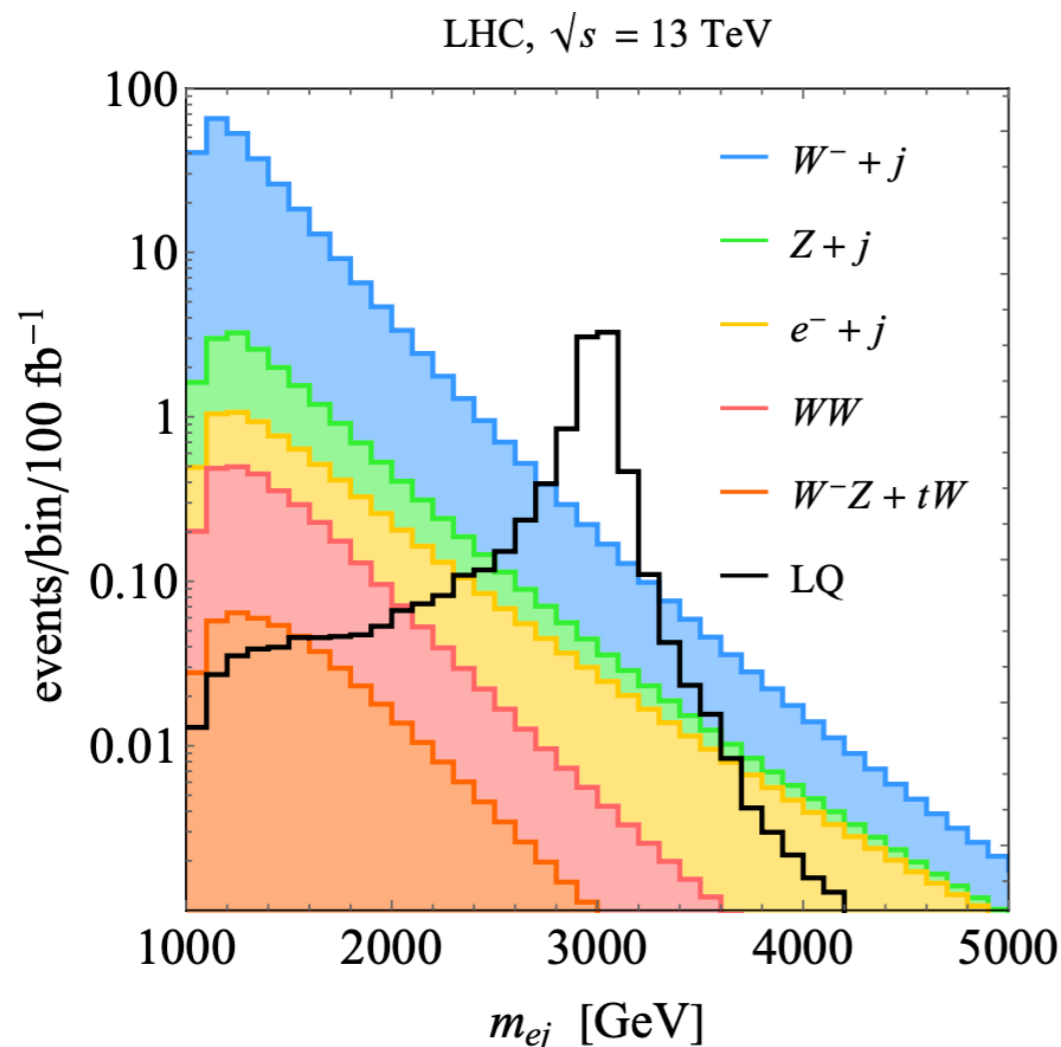
# LeptoQuarks Searches at LHC: s-channel production



Main background. Simulated at NLO(QCD)+PS (NNLO QCD + NLO EW should effectively reduce the cross section in the region of interest *J.M. Lindert et al* [[1705.04664](#)])

Suppressed by  $E_T$  miss requirement

# LeptoQuarks Searches at LHC: s-channel production



LQ signal exhibits a **mass peak** over a steeply falling background

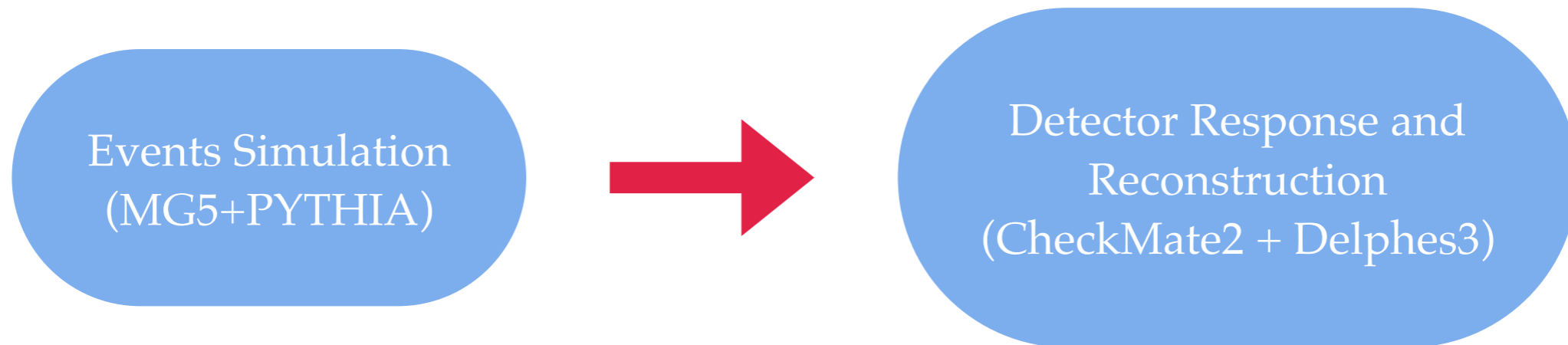
**Fake leptons** due to multi-jets misidentification and **mass resolution effects** must be included

## REMARKS

- PYTHIA does not handle lepton initiated processes. For the signal, we **trade leptons with photons** before showering. This leads to a **higher hadron activity** and hence a larger rejection (**conservative estimate**).
- We estimate the uncertainty to be of  $\mathcal{O}(10\%)$  by studying the process  $\gamma q \rightarrow e^- e^+ q$  and therefore the mis-modelling only mildly affects our analysis

# LeptoQuarks Searches at LHC: analysis details & follow-up

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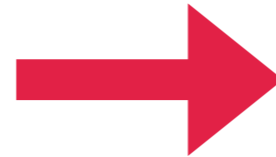
- **Multijet backgrounds:** incorporated as a systematic uncertainty taken from the ATLAS  $\ell + E_{T,\text{miss}}$  search [[1906.05609](#)] and doubling the quoted error.
- **Lepton-jet mass resolution:** estimated by combining the information on the dilepton & dijet mass resolutions given in [[1903.06248](#)] & [[1910.08447](#)].

**NEW**

- **Multijet backgrounds refinement:** background estimate and systematic uncertainty extrapolated from the ATLAS  $\ell + j$  search [[1311.2006](#)].
- Added PDF uncertainties on the main background
- Better estimate of lepton-jet mass resolution and of the broadening of the reconstructed LQ peak

# LeptoQuarks Searches at LHC: analysis details & follow-up

Events Simulation  
(MG5+PYTHIA)



Detector Response and  
Reconstruction  
(CheckMate2 + Delphes3)

- **Multijet backgrounds:** incorporated as a systematic uncertainty taken from the ATLAS  $\ell + E_{T,\text{miss}}$  search [[1906.05609](#)] and doubling the quoted error.
- **Lepton-jet mass resolution:** estimated by combining the information on the dilepton & dijet mass resolutions given in [[1903.06248](#)] & [[1910.08447](#)].

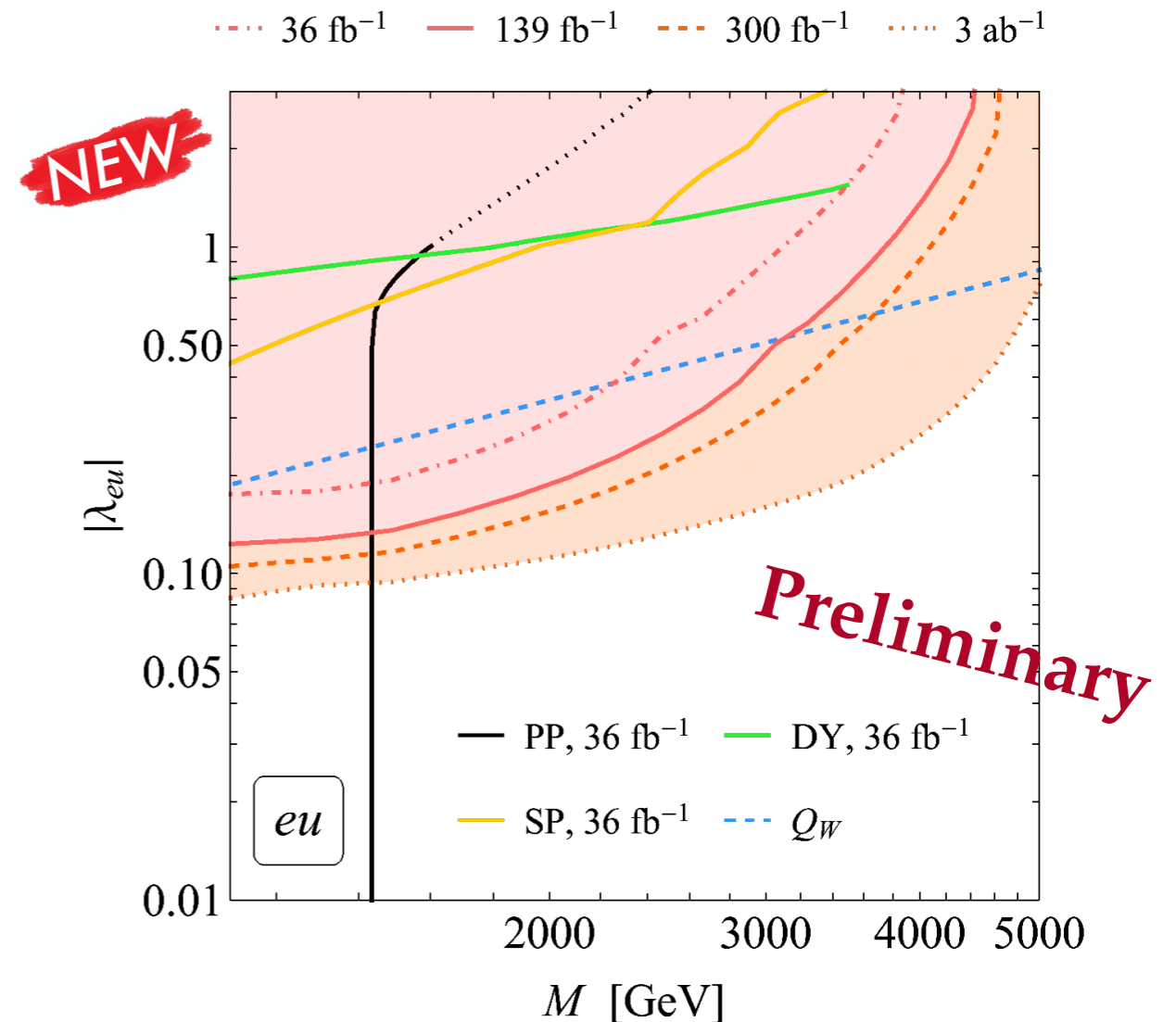
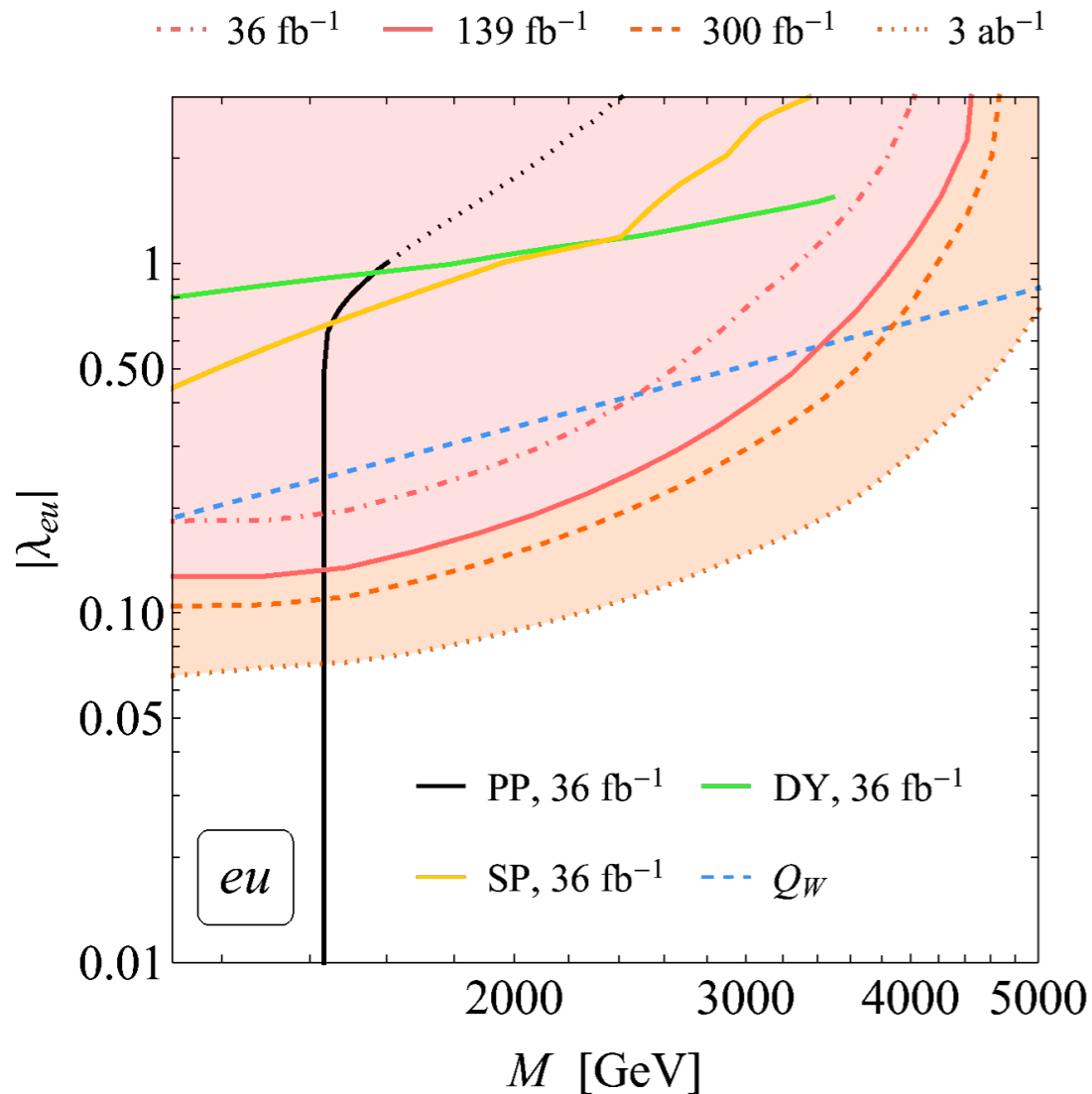
**NEW**

tot syst	1 TeV	2 TeV	3 TeV
e+j	7.6%	37%	143%
$\mu$ +j	9.4%	20%	65%

mass res	1 TeV	2 TeV	3 TeV
e+j	2.3%	1.7%	1.6%
$\mu$ +j	6.7%	12%	17%

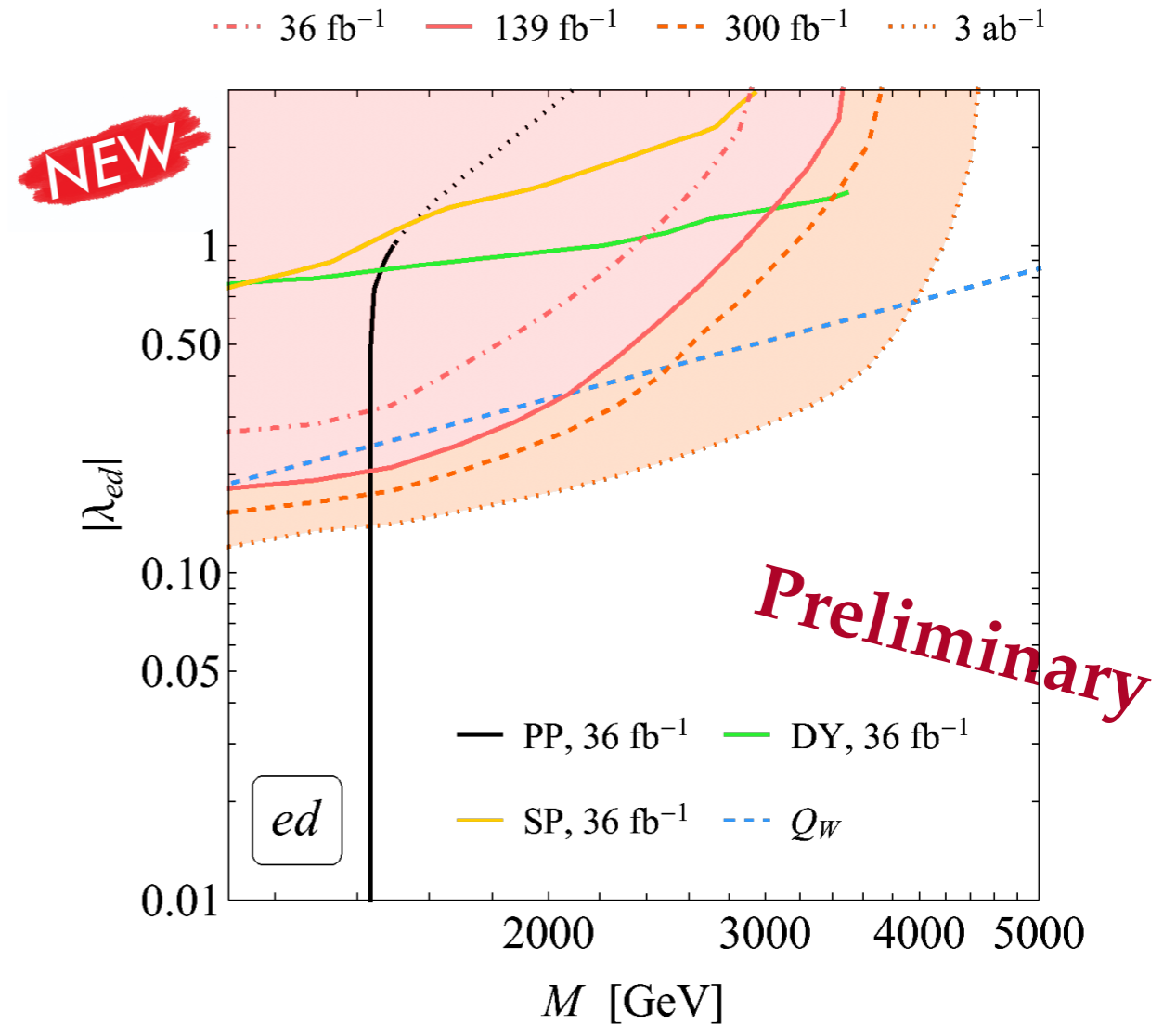
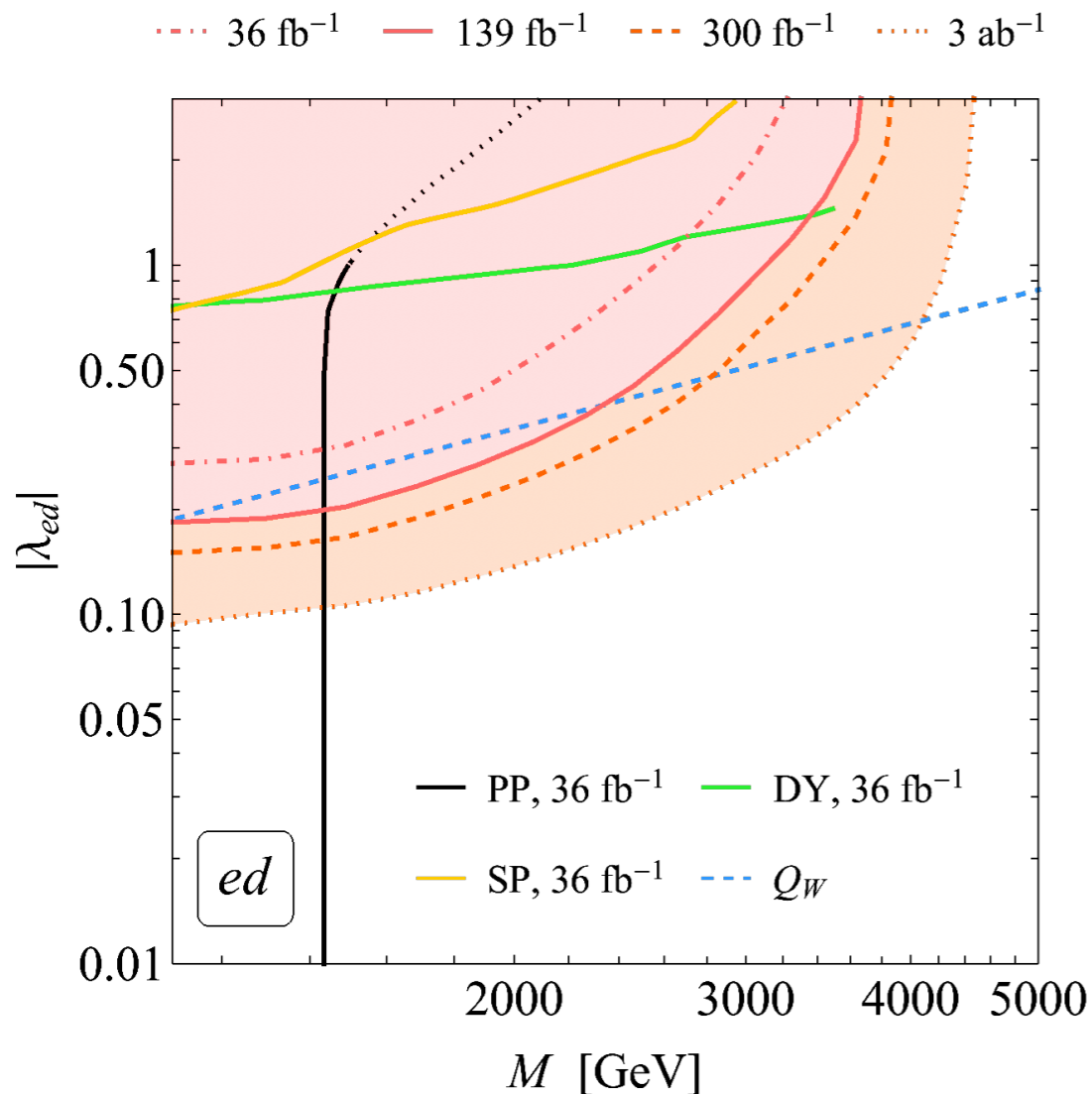


# LeptoQuarks Searches at LHC: $eu$ 95% CL limits



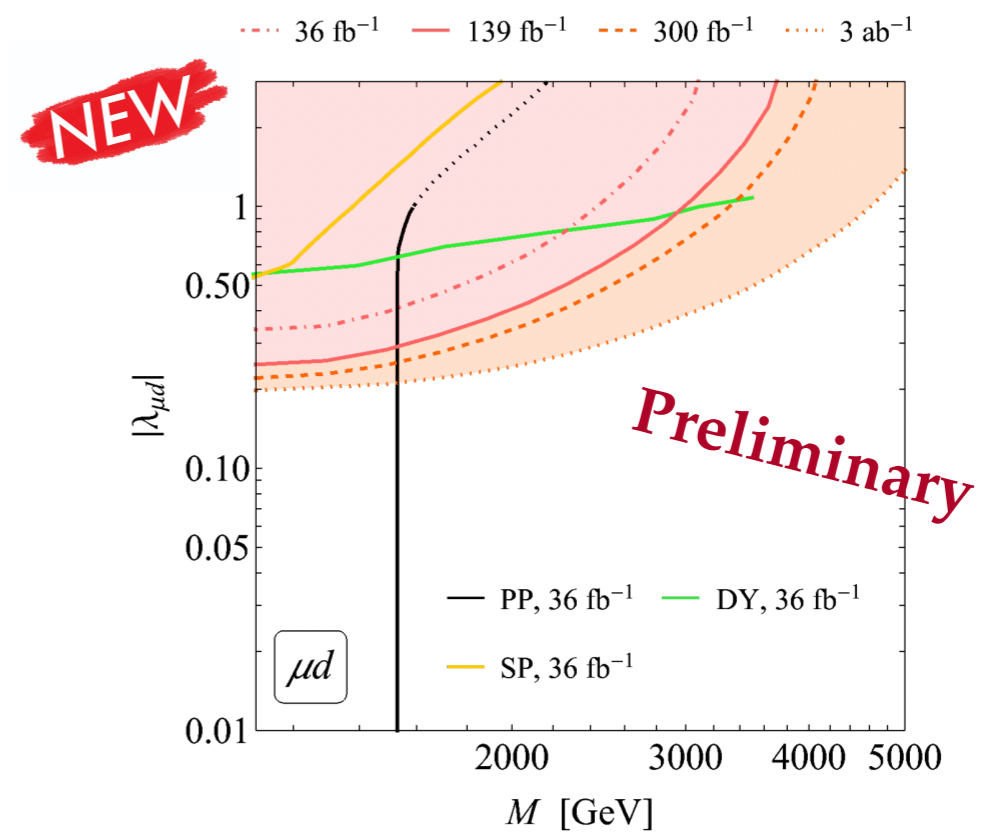
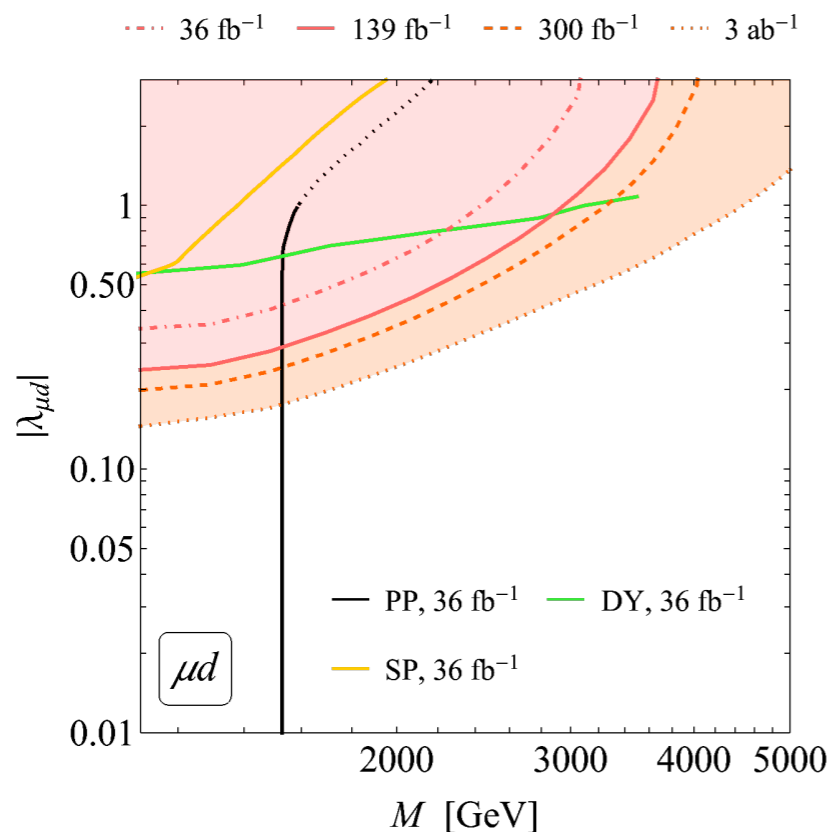
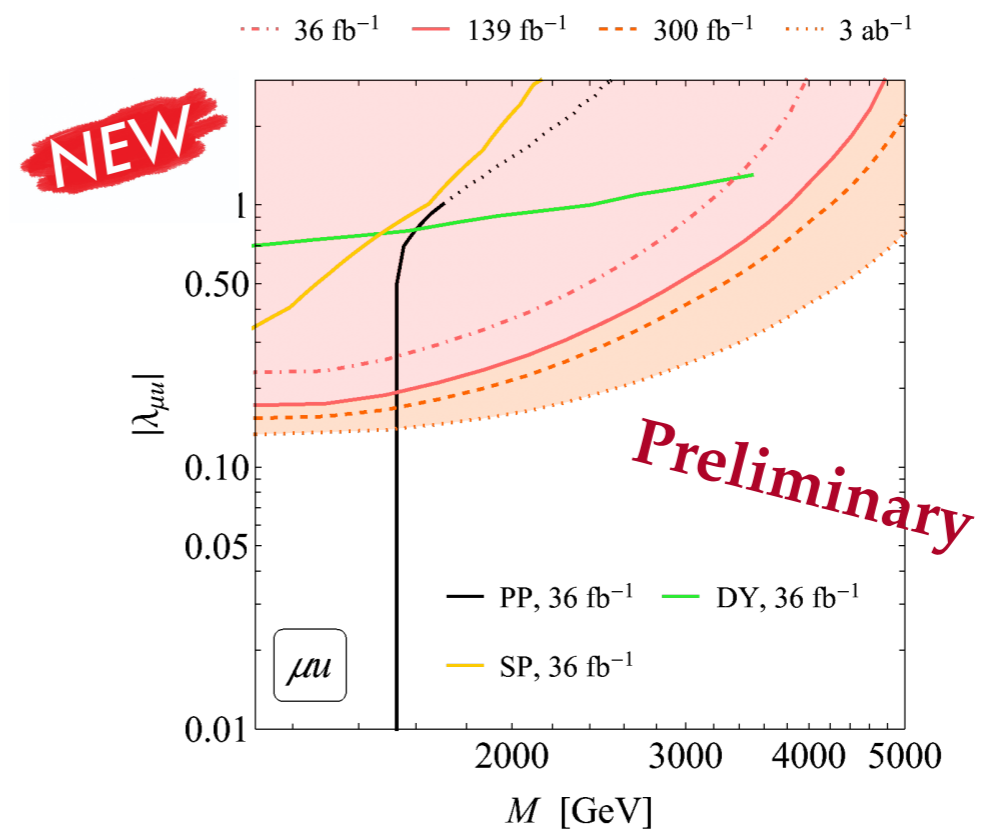
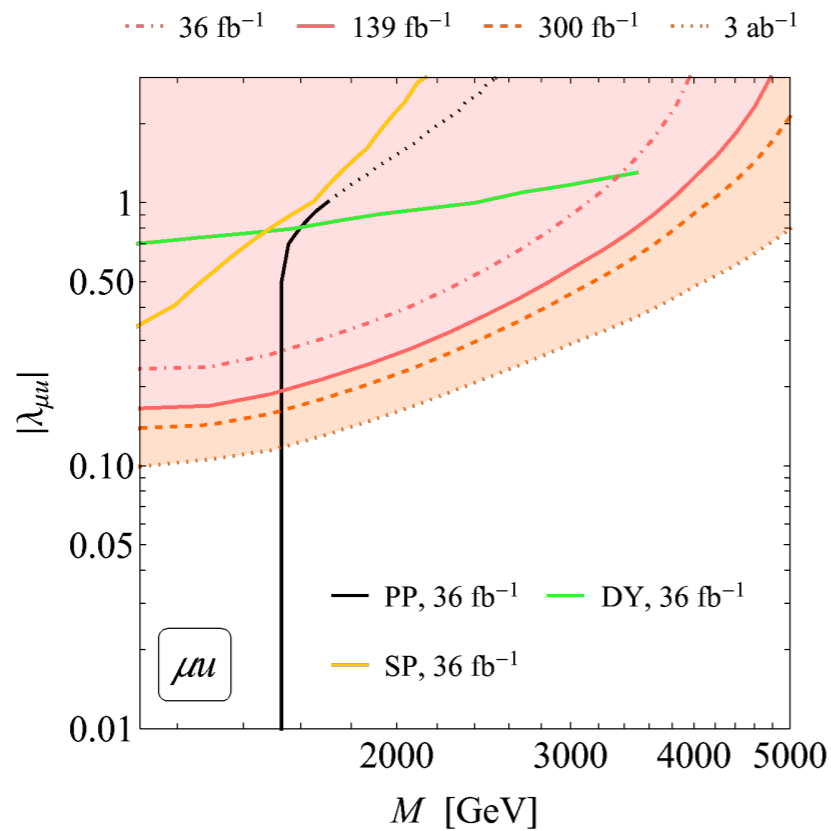
- Existing limits taken from [\[1810.10017\]](#)
- **Overall results are not spoiled** after the refinement of the analysis
- We get **stronger limits** than the ones arising from **atomic parity violation** and **parity-violating electron scattering experiments** for LQ masses up to 3 TeV (5 TeV) with the full Run II (HL-LHC).

# LeptoQuarks Searches at LHC: $ed$ 95% CL limits



- Analogous results for the limits on the  $\lambda_{ed}$  coupling. The limits are slightly weaker due to smaller  $d$  luminosity.
- We get **stronger limits** than the ones arising from **atomic parity violation** and **parity-violating electron scattering experiments** for LQ masses up to 2 TeV (4 TeV) with the full Run II (HL-LHC).

# LeptoQuarks Searches at LHC: $\mu q$ 95% CL limits



# CONCLUSIONS

---

- Lepton densities in the proton can be modelled with high precision using the LUX approach
- Using NLO lepton PDFs, lepton initiated processes are pushed to a level of accuracy comparable to the ones involving coloured partons
- NLO+PS implementations are within the reach. They are desirable to fully exploit the small hadron activity for background rejection
- A comment upon NLO corrections to lepton initiated processes:  $\mathcal{O}(\alpha)$ -photon induced processes must be included as NLO QCD. In essence, this is due to the relative importance of photon and lepton densities.

# CONCLUSIONS

---

- Despite the small cross sections
  - ✦ handful of SM lepton-lepton scattering events already produced with the full Run II luminosity and **might be measurable**
  - ✦ lepton initiated processes has **the potential to enlarge New Physics sensitivity in hadron collisions**
- General ideas for BSM searches
  - ✦ **simple resonant searches** for new interactions which **preferably** couple to leptons
  - ✦ enough **large couplings, exotic SM signatures** (to reduce background)
- We provide the first concrete example of a general search strategy for **resonant LQ production** induced by lepton PDFs
  - ✦ sensitive direct probe of 1st & 2nd-generation scalar LQs at the LHC
  - ✦ in view of its **simplicity** and **discovery reach**, ATLAS&CMS should performed dedicated resonance searches in lepton-jet final states

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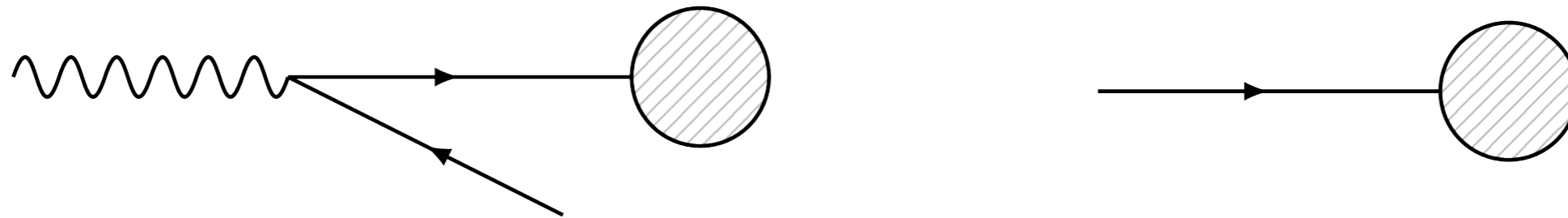
**BACKUP**

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# INTRODUCTION: MOTIVATIONS

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In general, lepton PDFs do not open new production mechanisms



4F vs 5F!

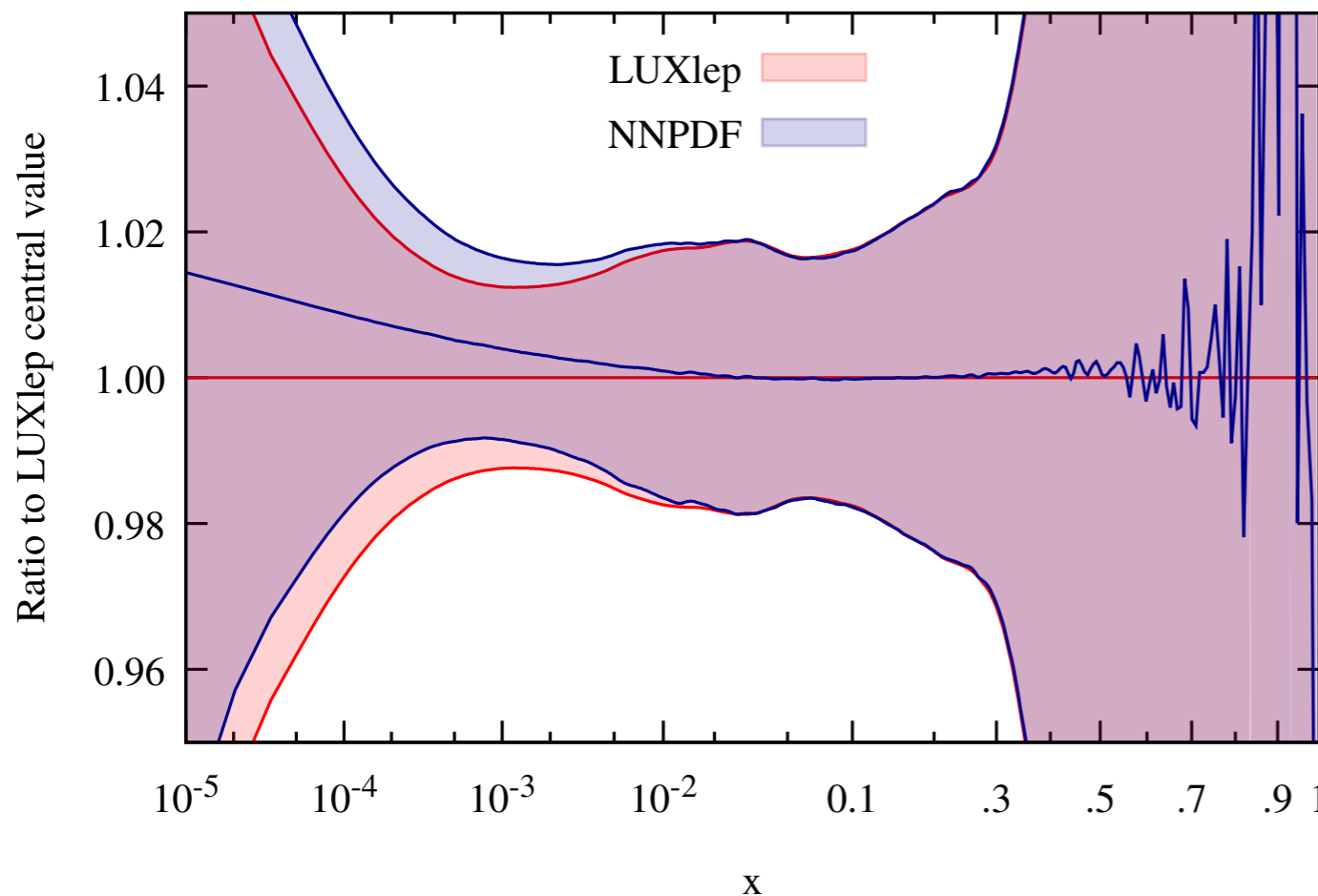
PROs

- Lepton masses very small (numerical instabilities). Potential large collinear  $\alpha \log \frac{Q}{m_\ell}$  effectively taken into account (and resummed in DGLAP)
- Smaller final state multiplicities
- Reduced hadronic activity (PS programs for lepton initiated processes required!)

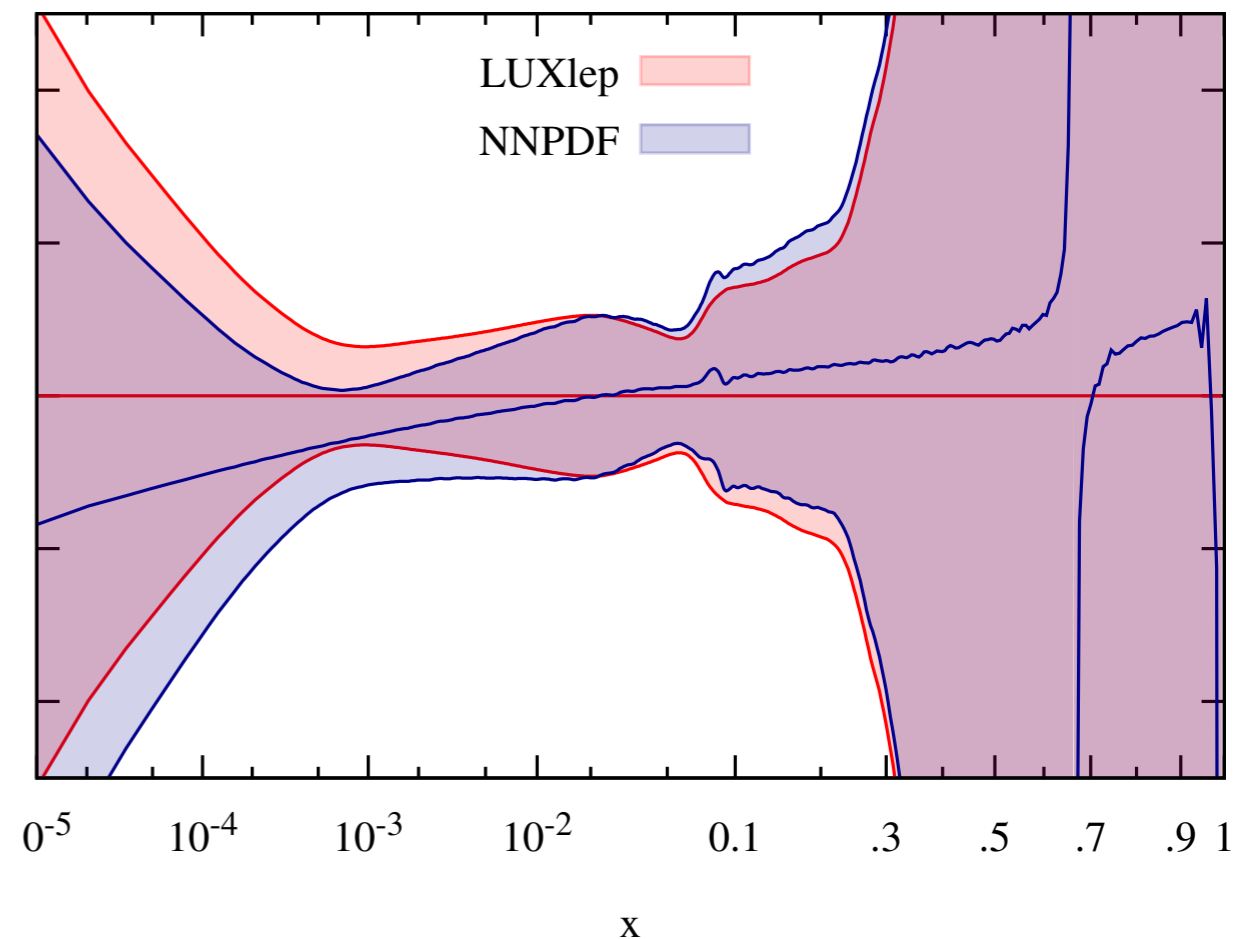
# COMPARISON among QUARK/GLUON PDFs

- Slightly differences (especially for gluons), within uncertainties
  - mainly due to the use of a different evolution framework (HOPPET)
  - effects of lepton PDF negligible on quark / gluon densities and momentum sum rule (sub per mille effect)

down density @  $\mu = 100$  GeV - total uncertainty



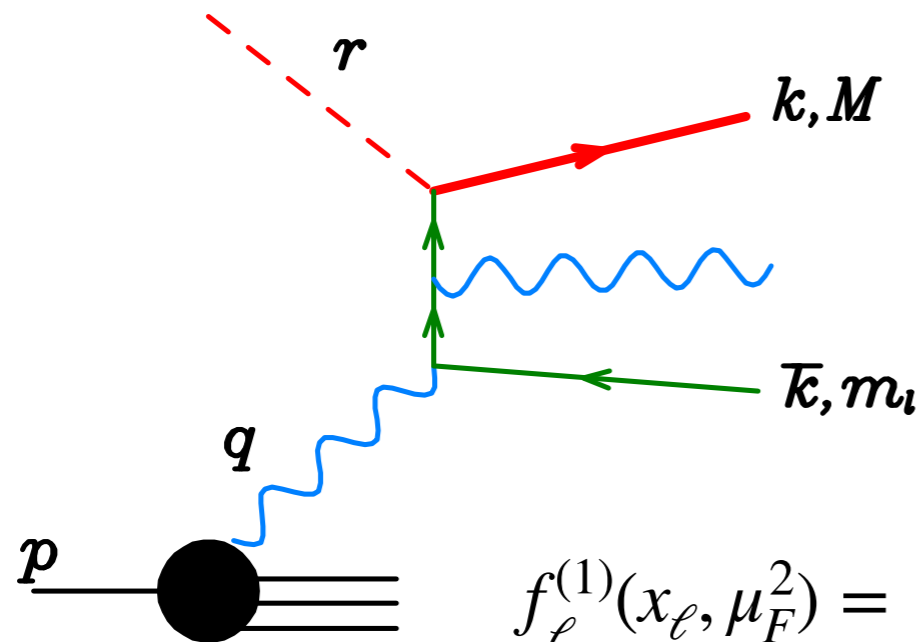
gluon density @  $\mu = 100$  GeV - total uncertainty





# $\mathcal{O}(\alpha^3 L^3)$ corrections

- We need to add only diagrams with photon emission off leptons
- The dominant contribution can be computed in the collinear approximations

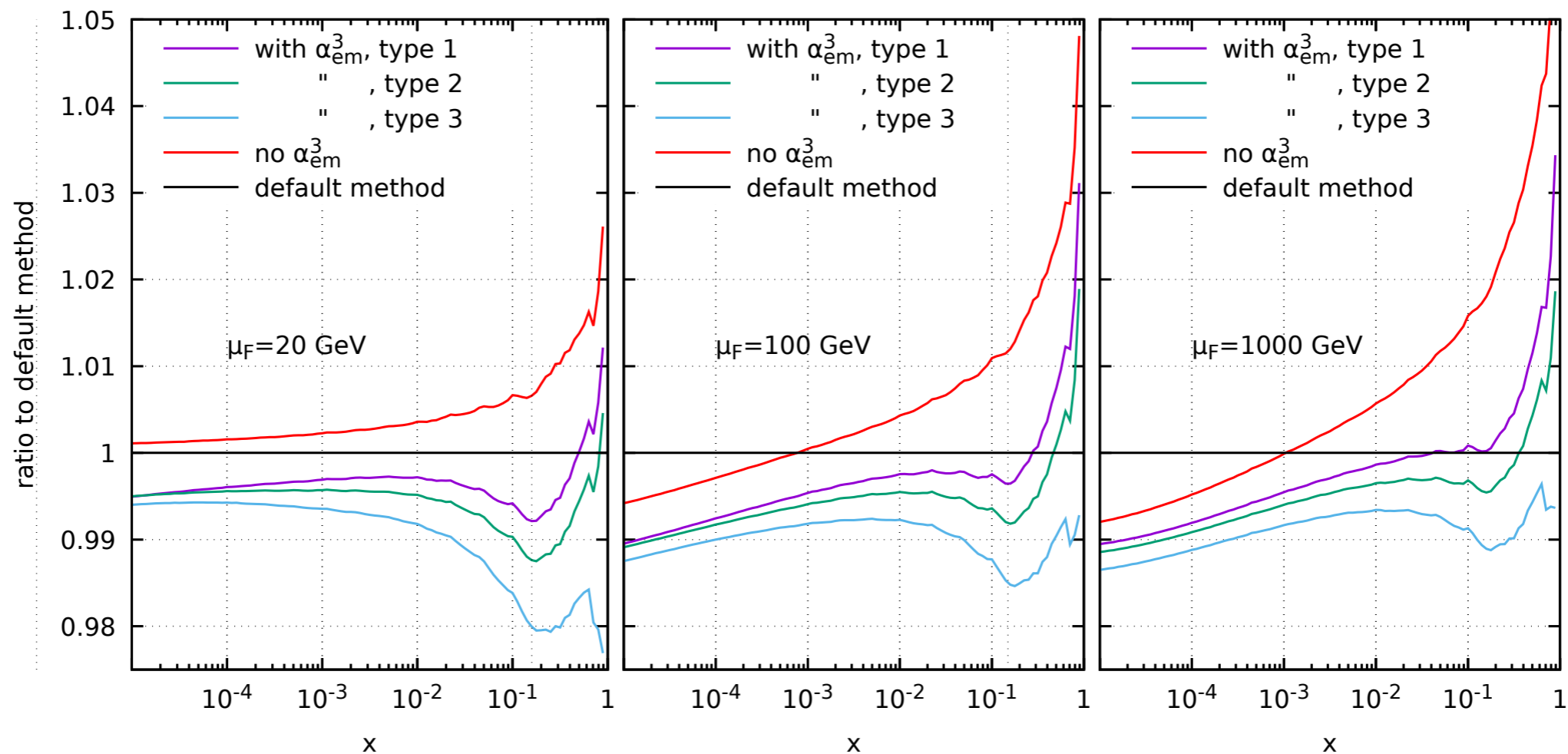


$$f_{\ell}^{(1)}(x_{\ell}, \mu_F^2) = \left(\frac{\alpha}{2\pi}\right)^3 \int_0^1 dx_{bj} \int_0^1 dz P_{\gamma q}(z) \int_0^1 dz_{\ell} P_{\ell\gamma}^{(2)}(z_{\ell})$$

$$\delta(x_{bj} z z_{\ell} - x_{\ell}) \int_{m_p^2}^{\mu_F^2} \frac{dQ^2}{Q^2} \sum_i f_i(x_{bj}, Q^2) c_i^2 \frac{1}{2} \log^2 \frac{M^2}{Q^2}$$

two explicit logs and one from  $Q^2$  integration. Here  $P_{\ell\gamma}^{(2)} = P_{\ell\ell} \otimes P_{\ell\gamma}$

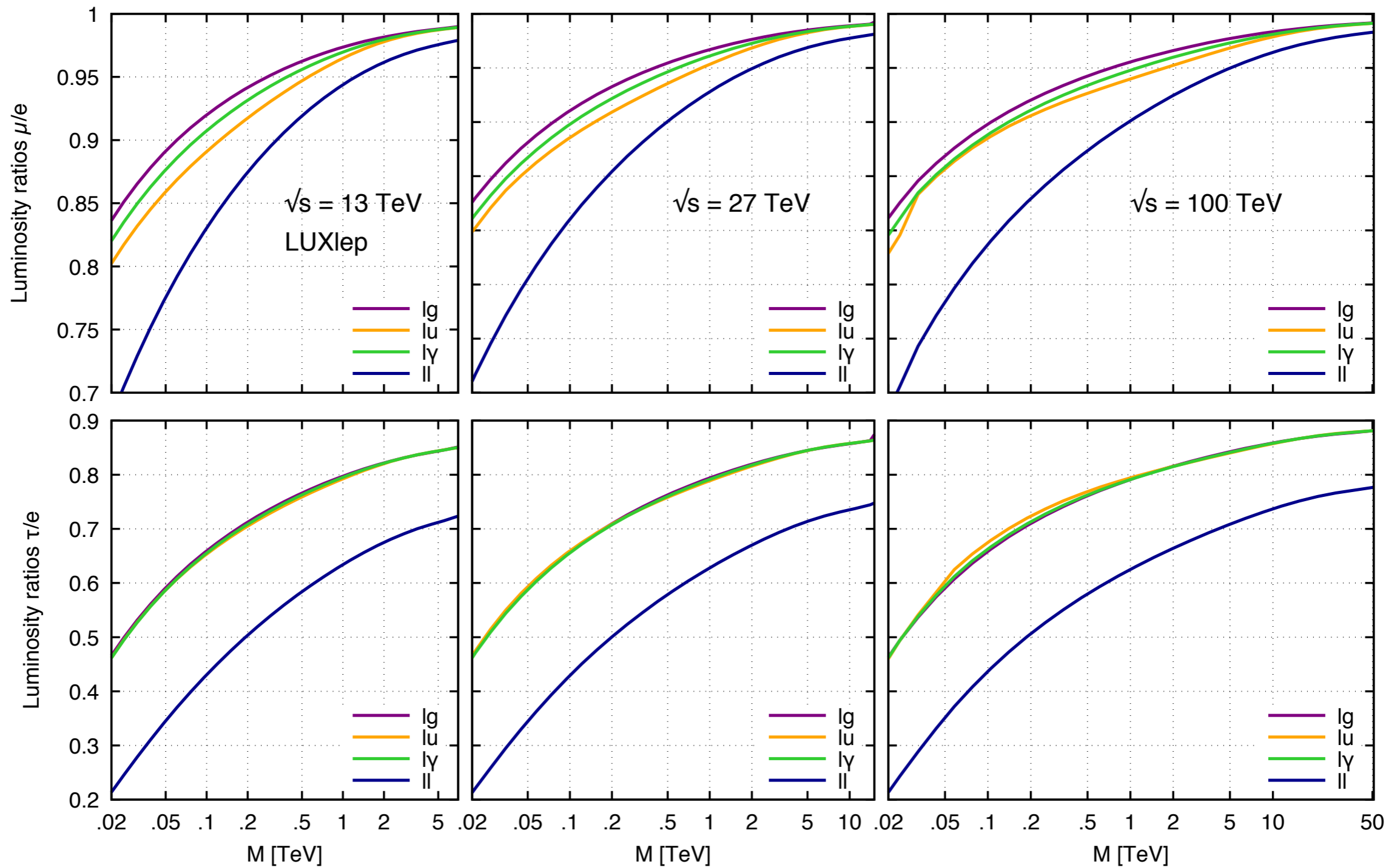
# $\mathcal{O}(\alpha^3 L^3)$ corrections - comparison with DGLAP



Our default method compared with three variants of the direct calculation of the  $\alpha^3 L^3$  terms. We conclude that

- The effect of the  $\alpha^3 L^3$  term is quite modest.
- There are large differences among the different method for its inclusion. This seems to indicate that sub-leading  $\alpha^3$  terms are not much smaller than the leading one.

# Luminosities for different leptons species



# CONSTRUCTION OF A FULL PDF WITH LEPTONS

---

- In practice, it's a bit more involved
  - we use a input NNPDF31\_nlo\_as\_0118 luxqed
  - we rely on HOPPET as DGLAP solver (different evolution framework, it does not include the  $P_{\ell q}$  splitting)
  - we add missing  $\alpha^3 L^3$  contributions through evolution

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  - we add missing  $\alpha^3 L^3$  contributions through evolution



1. Choose a reference scale where the Lepton (and Photon) PDF are extracted with our formula

**Remarks:**  $\mu_{\text{ref}}$  cannot be arbitrarily small, otherwise too sensitive to power suppression terms in  $Q^2$  (higher twist)

# CONSTRUCTION OF A FULL PDF WITH LEPTONS

---

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  - we rely on HOPPET as DGLAP solver (different evolution framework, it does not include the  $P_{\ell q}$  splitting)
  - we add missing  $\alpha^3 L^3$  contributions through evolution



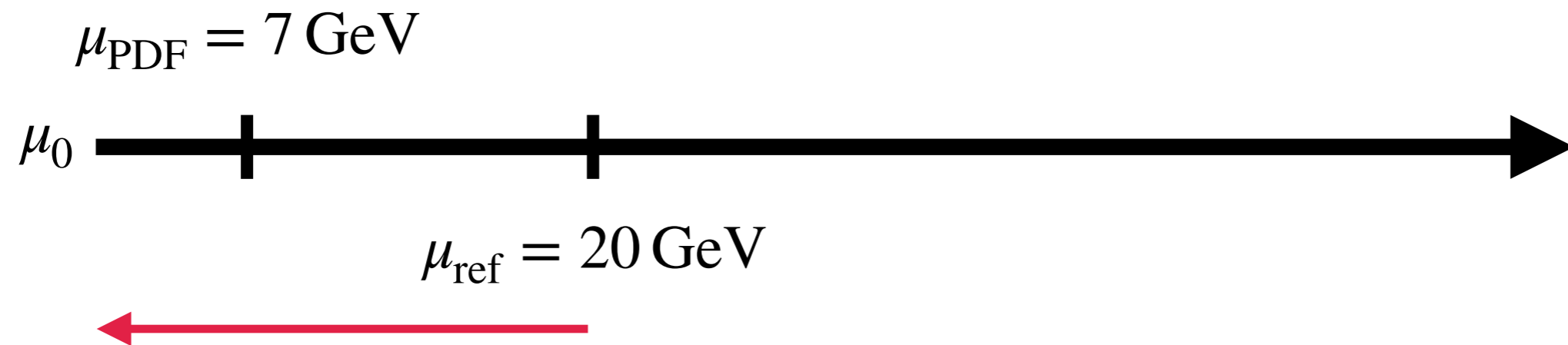
2. Choose a second scale  $\mu_{\text{PDF}}$  at which the original partons in NNPDF are loaded
3. Evolve from  $\mu_{\text{PDF}}$  to  $\mu_{\text{ref}}$  with all splitting turned on but the ones into leptons

**Remarks:** this is to avoid numerical instabilities due to the use of a different evolution program

# CONSTRUCTION OF A FULL PDF WITH LEPTONS

---

- In practice, it's a bit more involved
  - we use a input NNPDF31\_nlo\_as\_0118 luxqed
  - we rely on HOPPET as DGLAP solver (different evolution framework, it does not include the  $P_{\ell q}$  splitting)
  - we add missing  $\alpha^3 L^3$  contributions through evolution



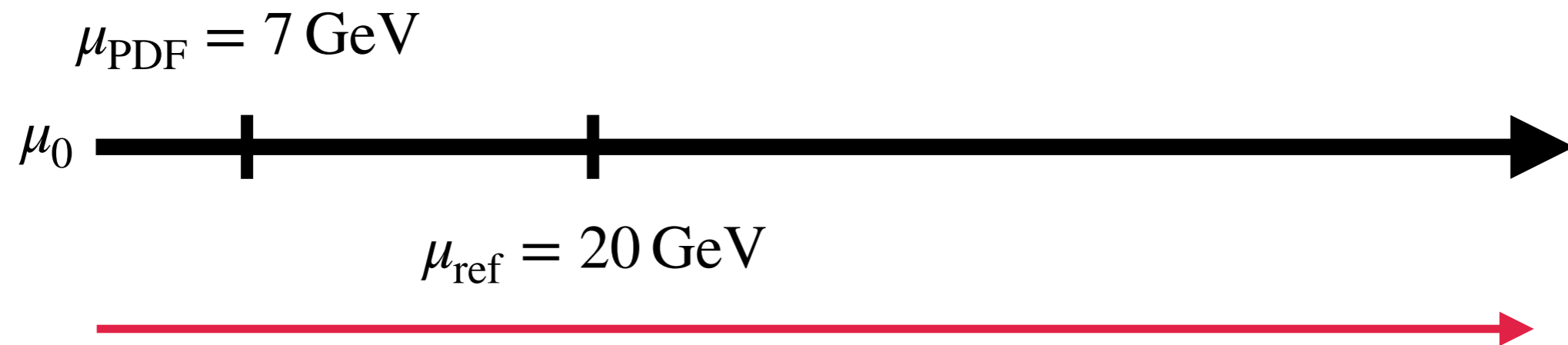
5. Add (replace) the lepton (photon) densities at  $\mu_{\text{ref}}$
6. Evolve down from  $\mu_{\text{ref}}$  to  $\mu_0$  with all splitting turned on but the  $P_{\ell\ell}$  which is responsible for the transition  $\ell \rightarrow \ell + \gamma$

**Remarks:** this matches our calculation of the lepton PDF

# CONSTRUCTION OF A FULL PDF WITH LEPTONS

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- In practice, it's a bit more involved
  - we use a input NNPDF31\_nlo\_as\_0118 luxqed
  - we rely on HOPPET as DGLAP solver (different evolution framework, it does not include the  $P_{\ell q}$  splitting)
  - we add missing  $\alpha^3 L^3$  contributions through evolution



7. Finally, evolve from  $\mu_0$  to all scales with the full set of splitting, including  $P_{\ell\ell}$

**Remarks:** in this way, we effectively take into account  $\alpha^3 L^3$  contributions